

# Modelling Snow Water Equivalent distribution in the Alps: the activities in Aosta Valley

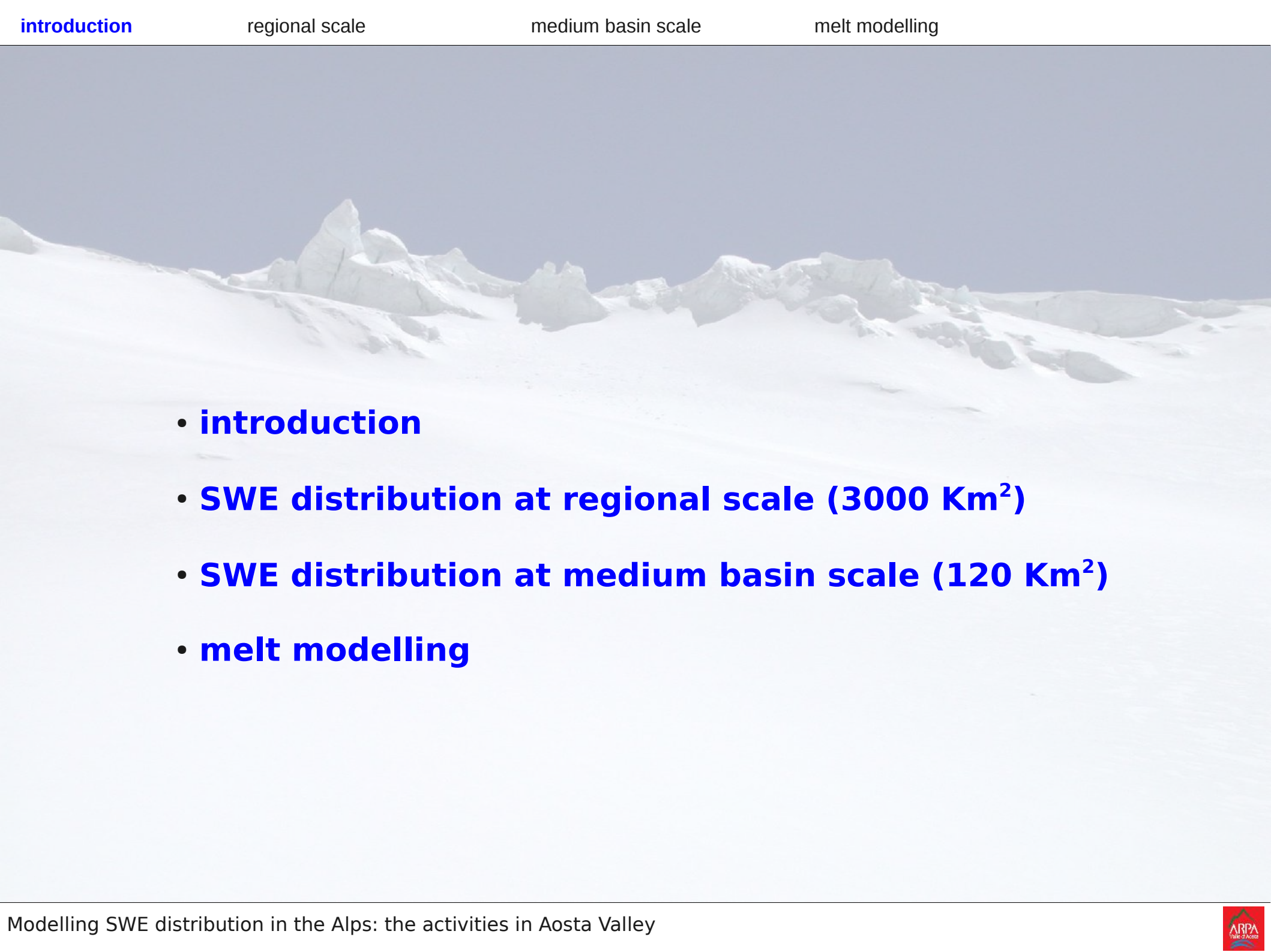
E. Cremonese<sup>(1)</sup>, P. Pogliotti<sup>(1,3)</sup>, U. Morra di Cella<sup>(1)</sup>, M. Galvagno<sup>(1,2)</sup>, F. Pellicciotti<sup>(4)</sup>

(1) - ARPA Valle d'Aosta

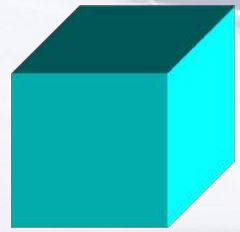
(2) - LTDA, DISAT – UNIMIB

(3) - GEOSITLAB, DST – UNITO

(4) - ETH - ZURICH

- 
- **introduction**
  - **SWE distribution at regional scale (3000 Km<sup>2</sup>)**
  - **SWE distribution at medium basin scale (120 Km<sup>2</sup>)**
  - **melt modelling**

$$\text{SWE} = \text{SNOW HEIGHT} \times \text{SNOW COVER} \times \text{SNOW DENSITY}$$



SWE [mm w.e.]

=



$H_s$  [m]

x

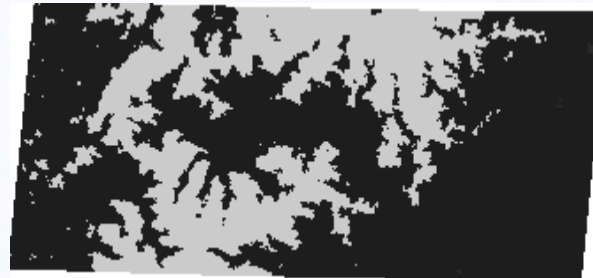


SCA [m<sup>2</sup>]

x



$\rho_s$  [kgm<sup>-3</sup>]



introduction

**SWE distribution at regional scale (3000 Km<sup>2</sup>)**

SWE distribution at medium basin scale (120 Km<sup>2</sup>)

melt modelling



## **SWE at regional scale**

**the aim is to know the evolution of total amount and distribution of SWE on the Aosta Valley during the winter time**

**it's used for the hydrological bulletin & it's an important information for summer drought crisis (e.g. Autorità di Bacino del Po)**

**it's done with a monthly frequency from November to June**

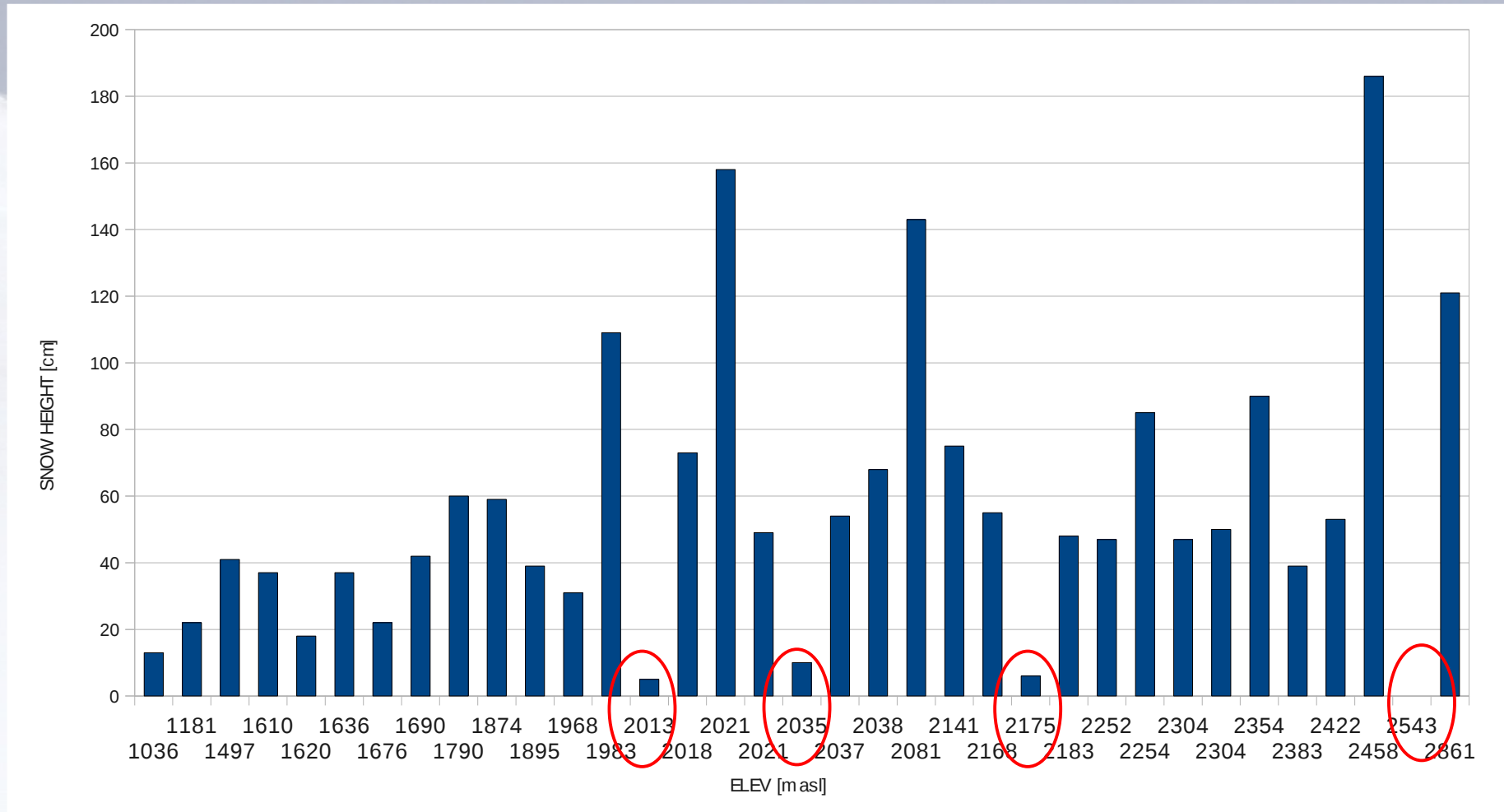
$$\text{SWE} = \text{SNOW HEIGHT} \times \text{SNOW DENSITY} \times \text{SNOW COVER EXTENT}$$

**SNOW HEIGHT: from point measurements to distributed fields**



**Automatic snow height measurements point (ultrasonic depth gauge) in Aosta Valley (n=35)  
... continuous measurements**

## SNOW HEIGHT: from point measurements to distributed fields



**Data reliability !!**

## SNOW HEIGHT: from point measurements to distributed fields



**Data reliability !!**

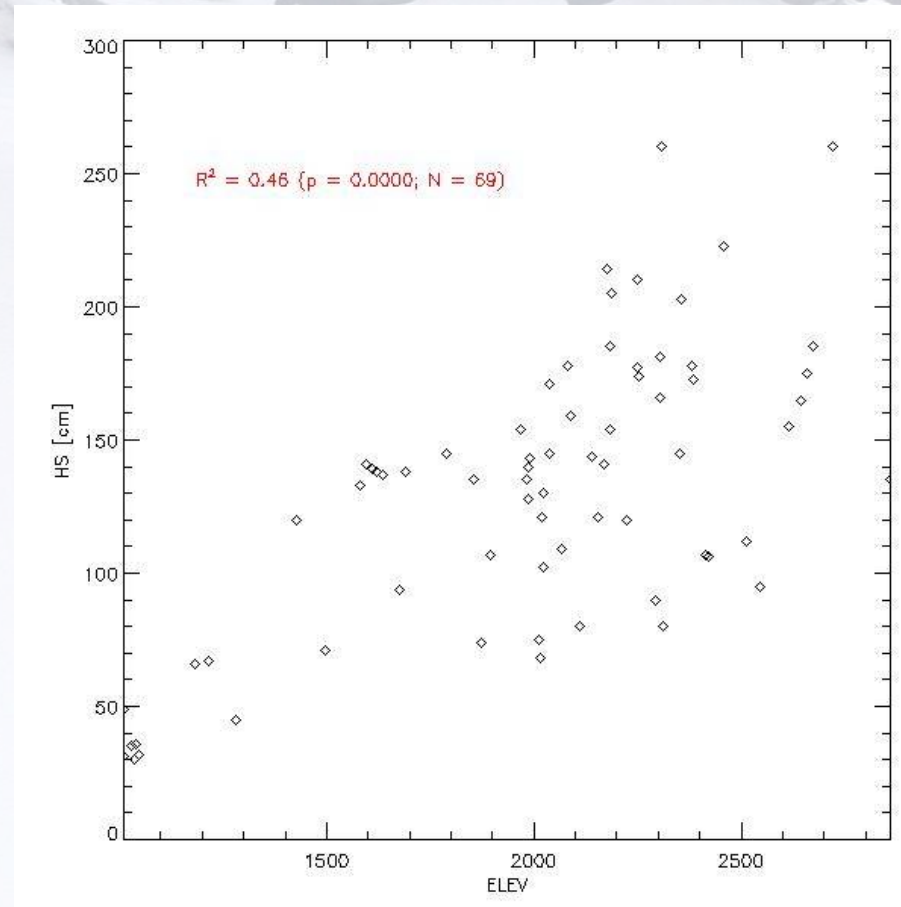


## SNOW HEIGHT: from point measurements to distributed fields

How can we move from **point measurements** to a snow height value **distributed** all over the entire Aosta Valley?

# SNOW HEIGHT: from point measurements to distributed fields

We try to find **empirical relationships** between snow height and some morphological parameters (e.g. at higher elevation we have a thicker snow height)



# SNOW HEIGHT: from point measurements to distributed fields

We try to find **empirical relationships** between snow height and some morphological parameters

## Steps

- 1) **model definition: GLM:  $y = \alpha + \beta_1 x_1 + \dots + \beta_n x_n + \varphi$**
- 2) **selection of the morphological parameters ( $x_1, x_2, \dots$ ) to include in the model (Akaike Information Criteria – AIC)**
- 3) **model coefficients ( $\beta_1, \beta_n, \dots$ ) estimation by bootstrap procedure**
- 4) **model evaluation by cross validation techniques (LGO and k-fold)**
- 5) **analysis of the crossvalidated statistics ( $R^2_{cv}, EF_{cv}, RMSE_{cv}$ )**

## SNOW HEIGHT: from point measurements to distributed fields

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### DISTRIBUTED PARAMETERS

Elevation

Slope

Exposition

Northness index

Concavity/Convexity

Monthly Direct Radiation

Monthly Diffuse Radiation

Monthly Global Radiation

Monthly Direct Radiation Duration

# SNOW HEIGHT: from point measurements to distributed fields

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DEM

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DISTRIBUTED PARAMETERS	
Elevation	
Slope	
Exposition	
Northness index	
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Monthly Direct Radiation	
Monthly Diffuse Radiation	
Monthly Global Radiation	
Monthly Direct Radiation Duration	

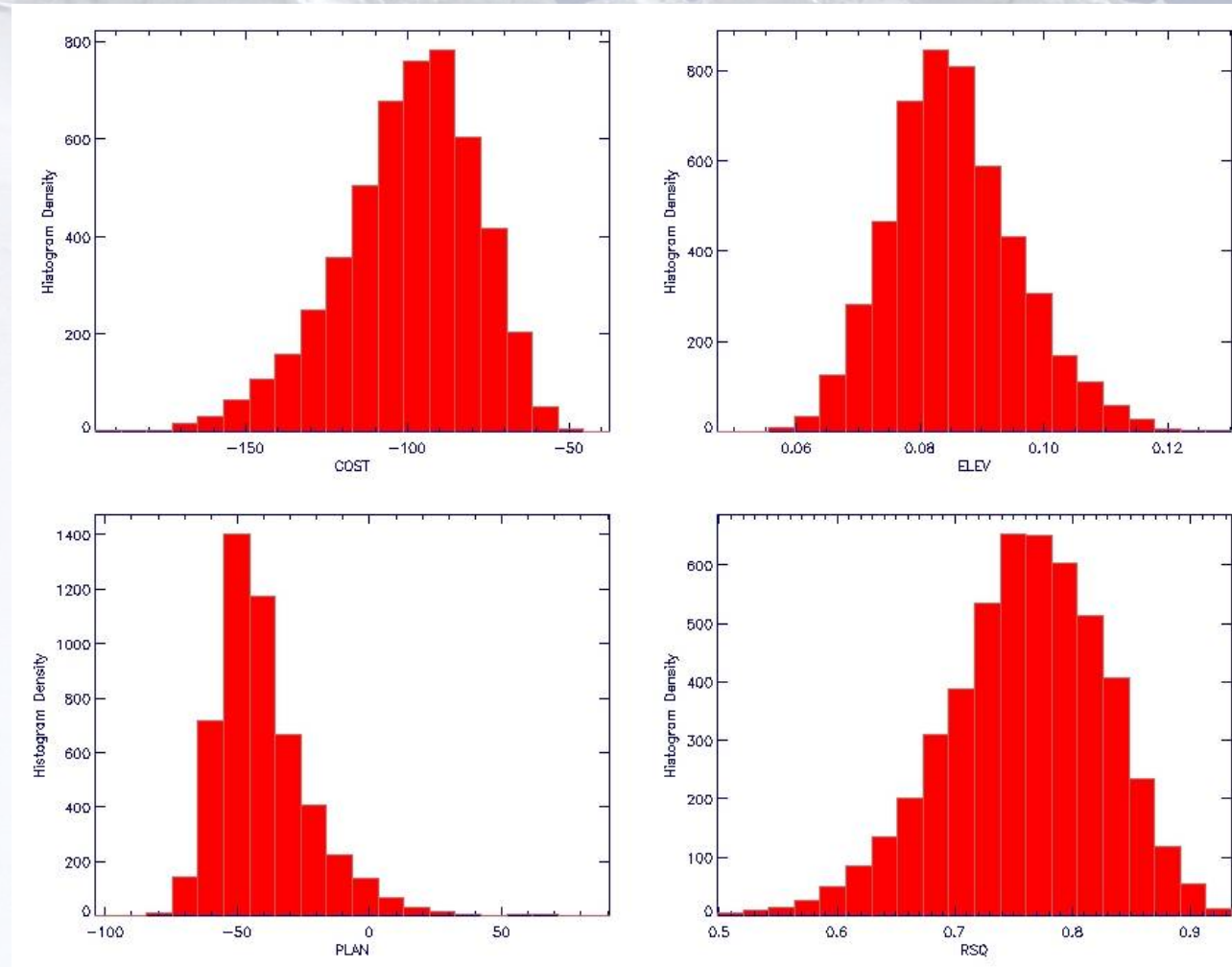
DEM

DEM + solar radiation model

# SNOW HEIGHT: from point measurements to distributed fields

November 2008: selected parameters by AIC:  
 $SH = COST + \beta_1 ELEV + \beta_2 CONC/CONV$

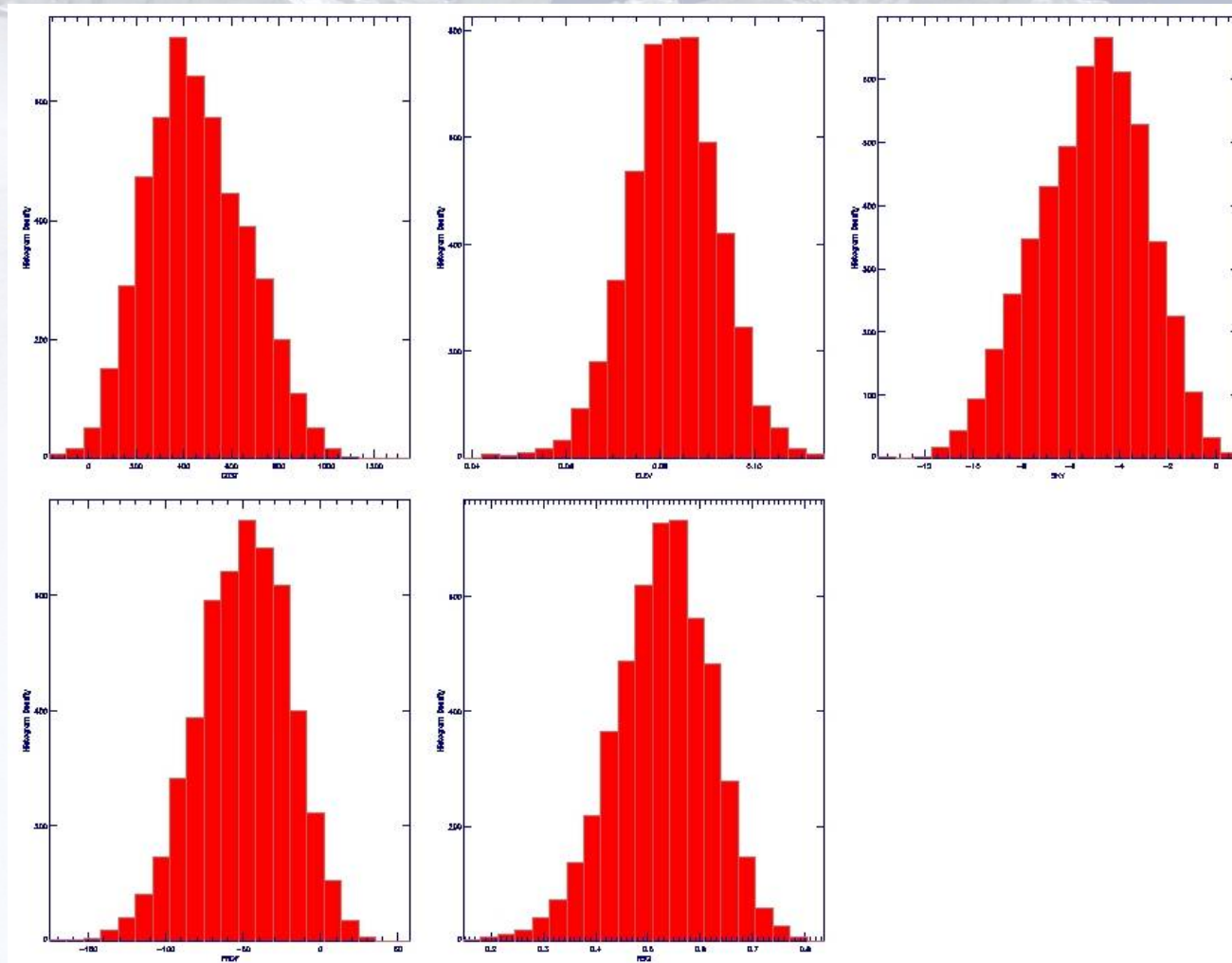
3) model coefficients ( $\beta_1, \beta_n, \dots$ ) estimation by bootstrap procedure



# SNOW HEIGHT: from point measurements to distributed fields

December 2008: selected parameters by AIC:  
 $SH = COST + \beta_1 ELEV + \beta_2 SVF + \beta_3 CONC/CONV$

3) model coefficients ( $\beta_1, \beta_n, \dots$ ) estimation by bootstrap procedure



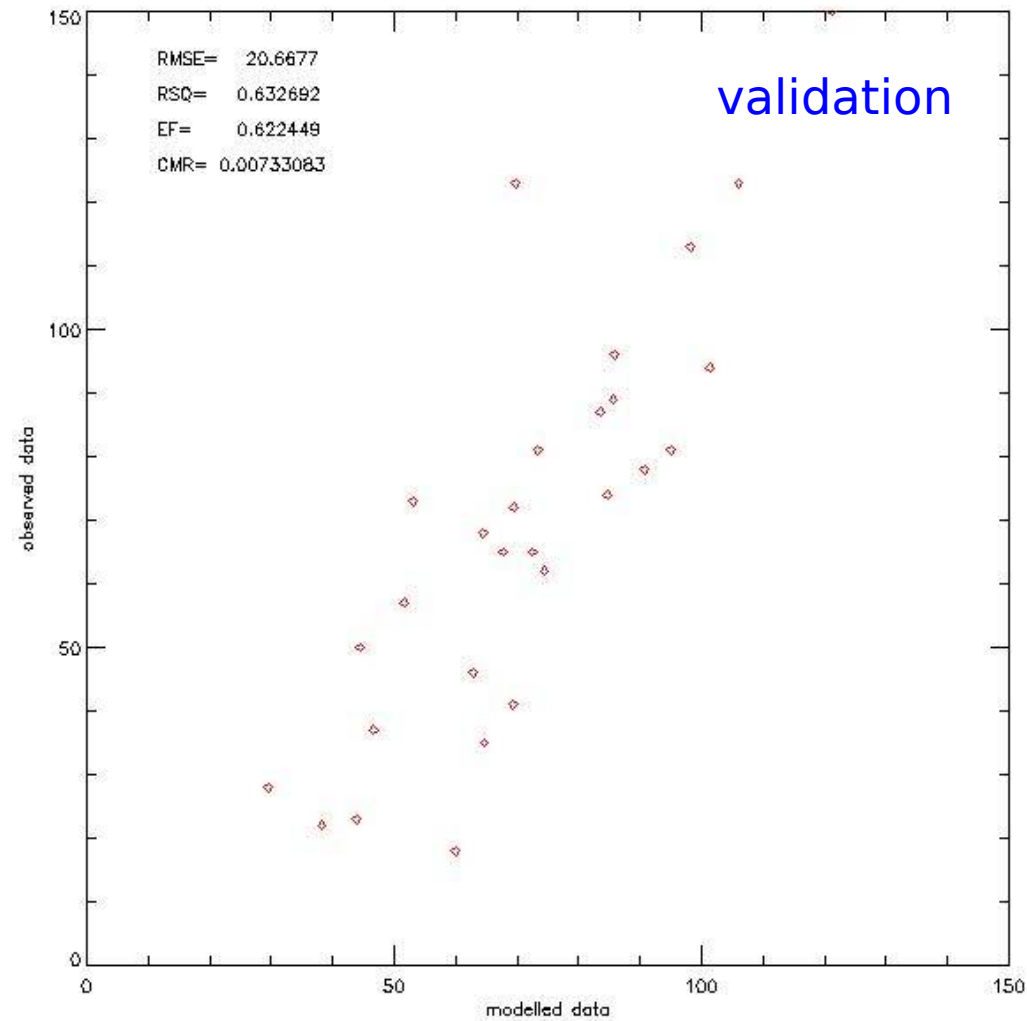
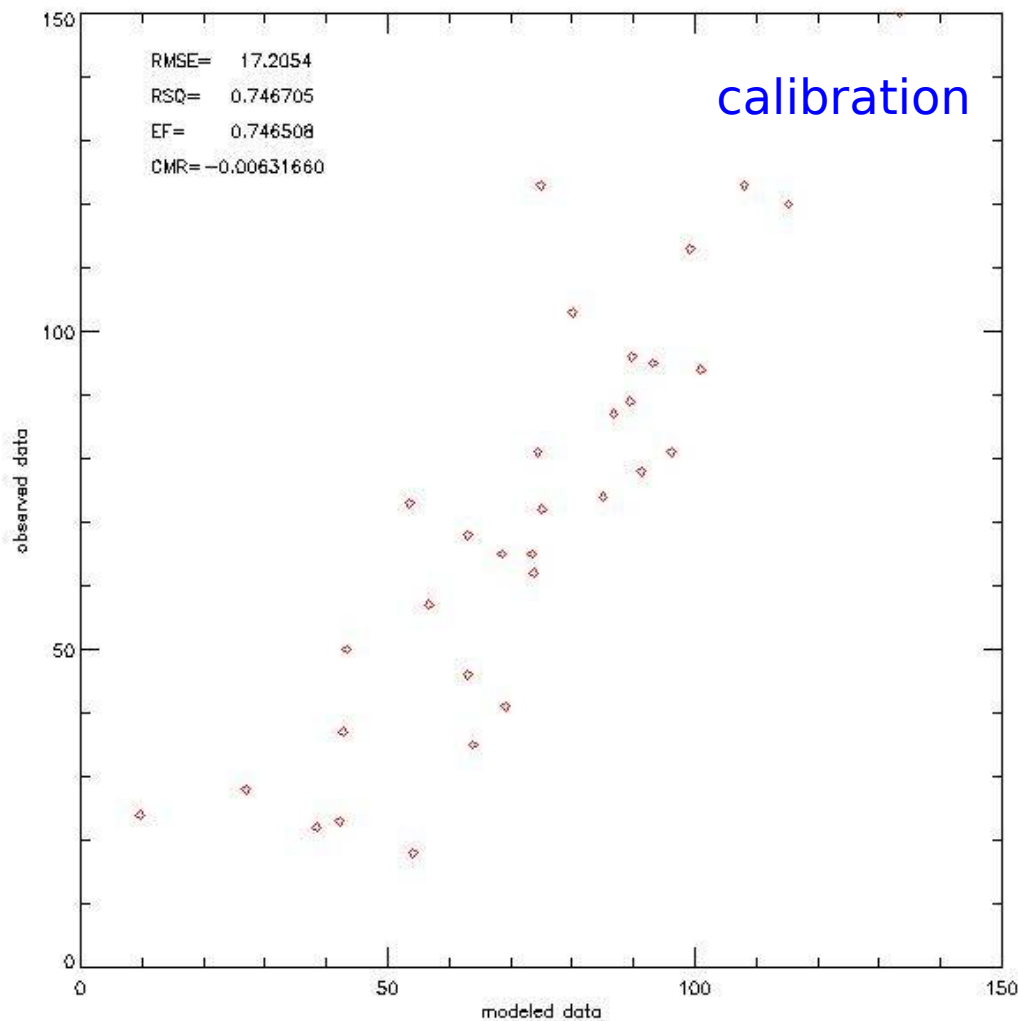


# SNOW HEIGHT: from point measurements to distributed fields

4) model evaluation by **cross validation** techniques (LGO and k-fold)

5) **analysis of the crossvalidated statistics** ( $R^2_{cv}$ ,  $EF_{cv}$ ,  $RMSE_{cv}$ )

e.g. December 2008



# SNOW HEIGHT: from point measurements to distributed fields

4) model evaluation by **cross validation** techniques (LGO and k-fold)

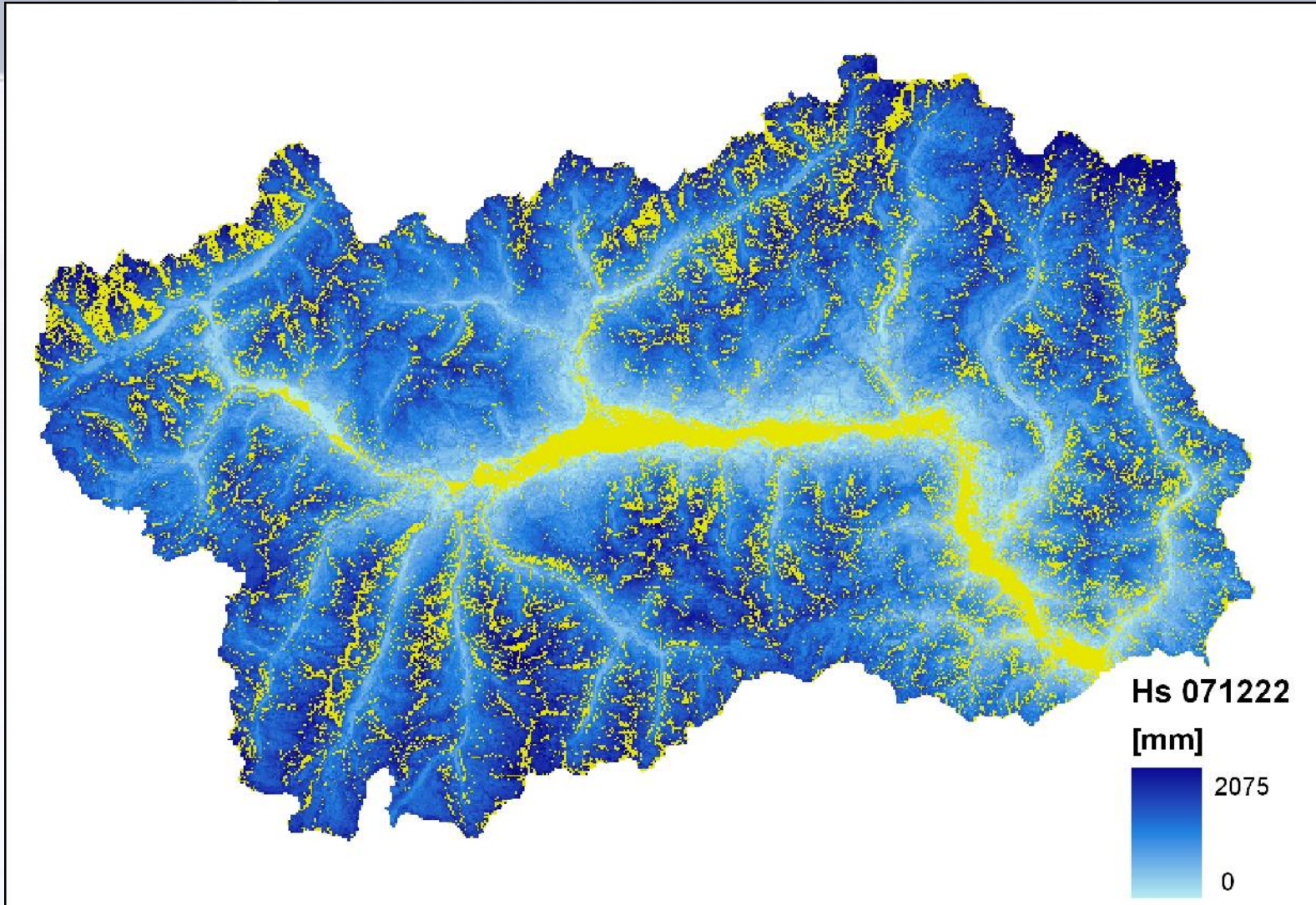
5) **analysis of the crossvalidated statistics** ( $R^2_{cv}$ ,  $EF_{cv}$ ,  $RMSE_{cv}$ )

## Model evaluation statistics in time

	$RMSE_{cl}$	$RMSE_{cv}$	$R^2_{cl}$	$R^2_{cv}$	$EF_{cl}$	$EF_{cv}$
mar 2008	51	62	0.518	0.440	0.507	0.158
feb 2008	33	41	0.467	0.409	0.461	-0.014
jan 2008	36	40	0.395	0.352	0.394	-0.148
....						
nov 2008	36	39	0.522	0.448	0.520	0.344
dec 2008	16	19	0.744	0.741	0.744	0.623
jan 2009		33		0.630		0.487
feb 2009		41		0.643		0.508
mar 2009		46		0.455		0.377
apr 2009		60		0.487		0.339
...						

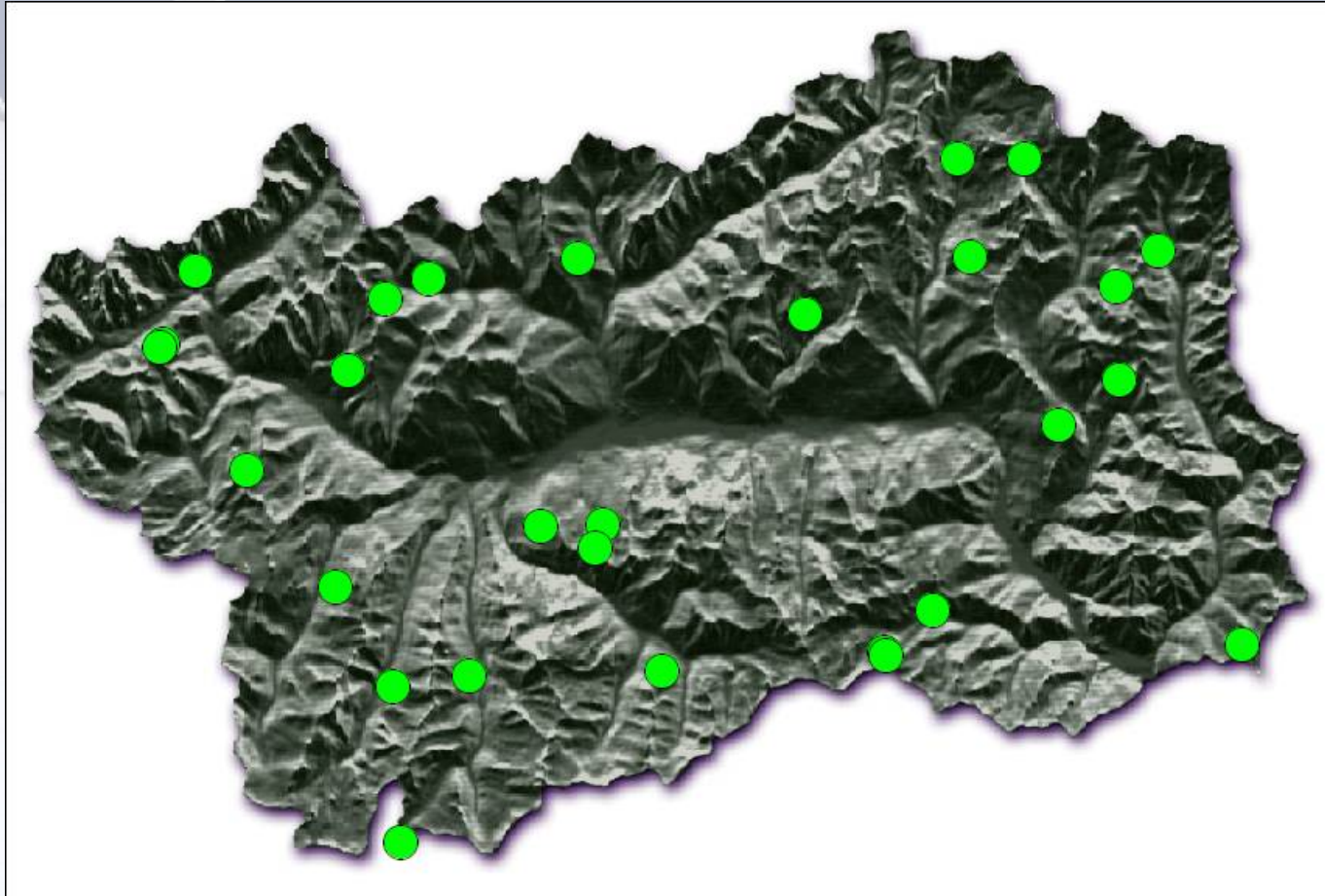
# SNOW HEIGHT: from point measurements to distributed fields

## Results of model application



**SWE = SNOW HEIGHT × SNOW DENSITY × SNOW COVER EXTENT**

**SNOW DENSITY: from point measurements to distributed fields**



**Manual measurements from snow pits, made for snow avalanches risk**

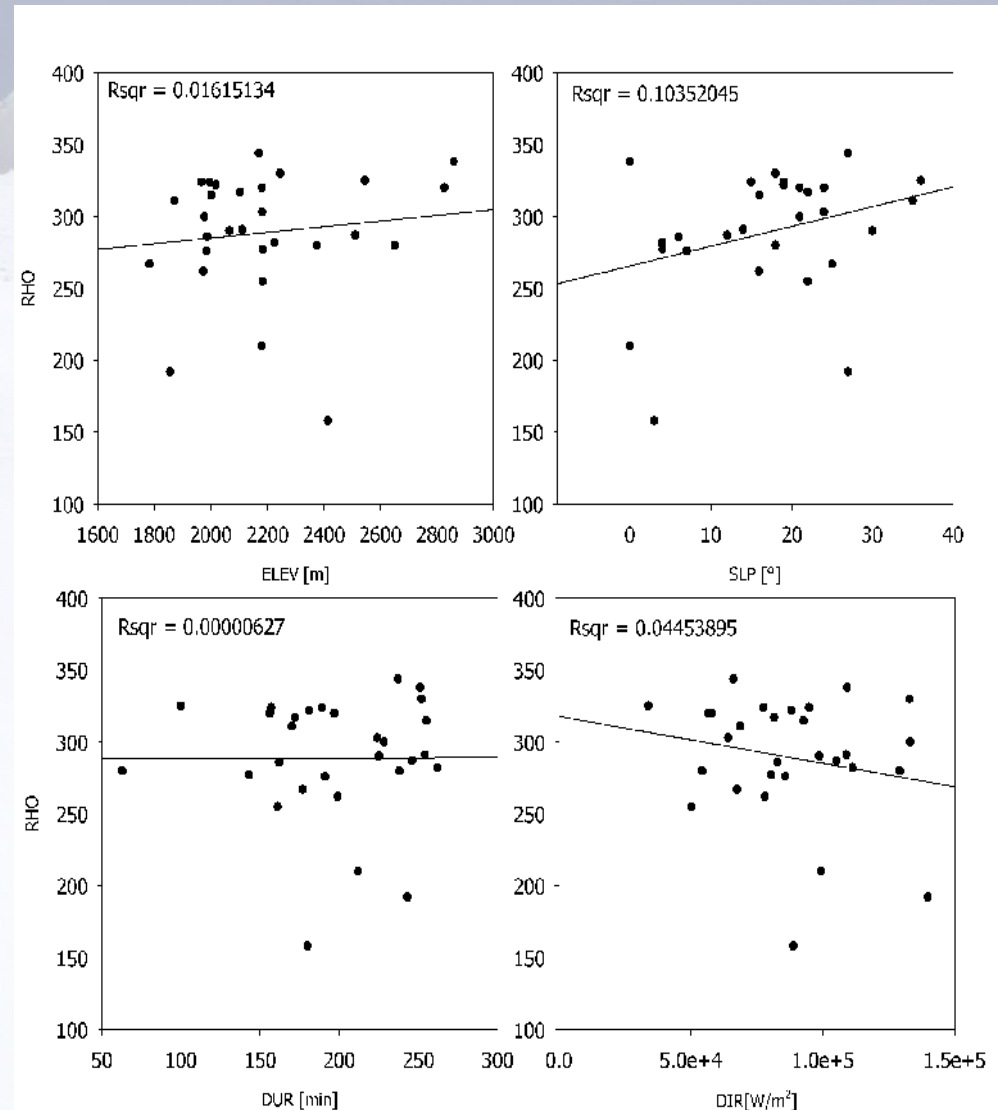
$$\text{SWE} = \text{SNOW HEIGHT} \times \text{SNOW DENSITY} \times \text{SNOW COVER EXTENT}$$

## SNOW DENSITY: from point measurements to distributed fields

in theory we can use the same modelling approach used for snow height

... in practice we have

...1) weak relationships with distributed parameters



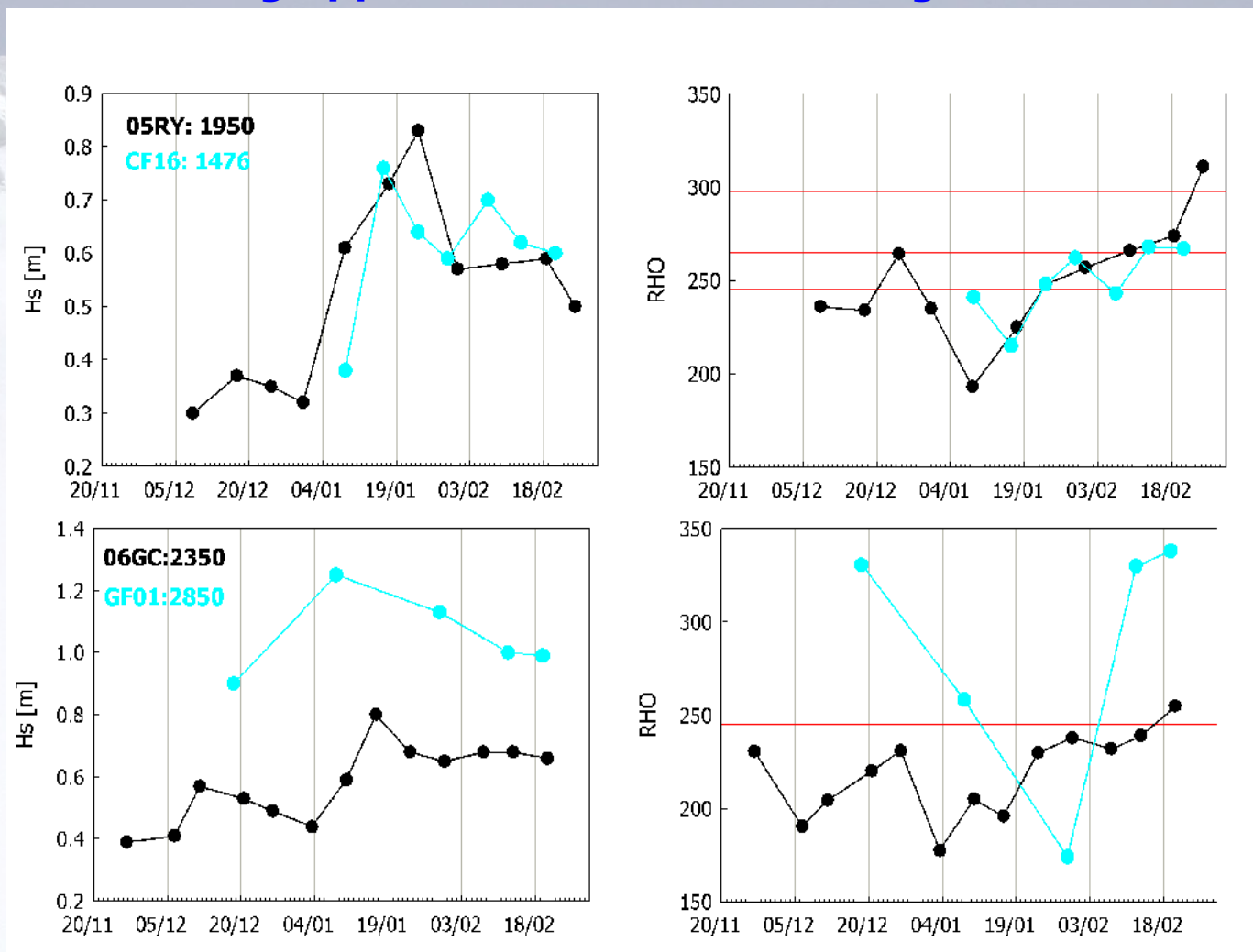
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## SNOW DENSITY: from point measurements to distributed fields

in theory we can use the same modelling approach used for snow height

... in practice we have

...2) bigger data reliability problems



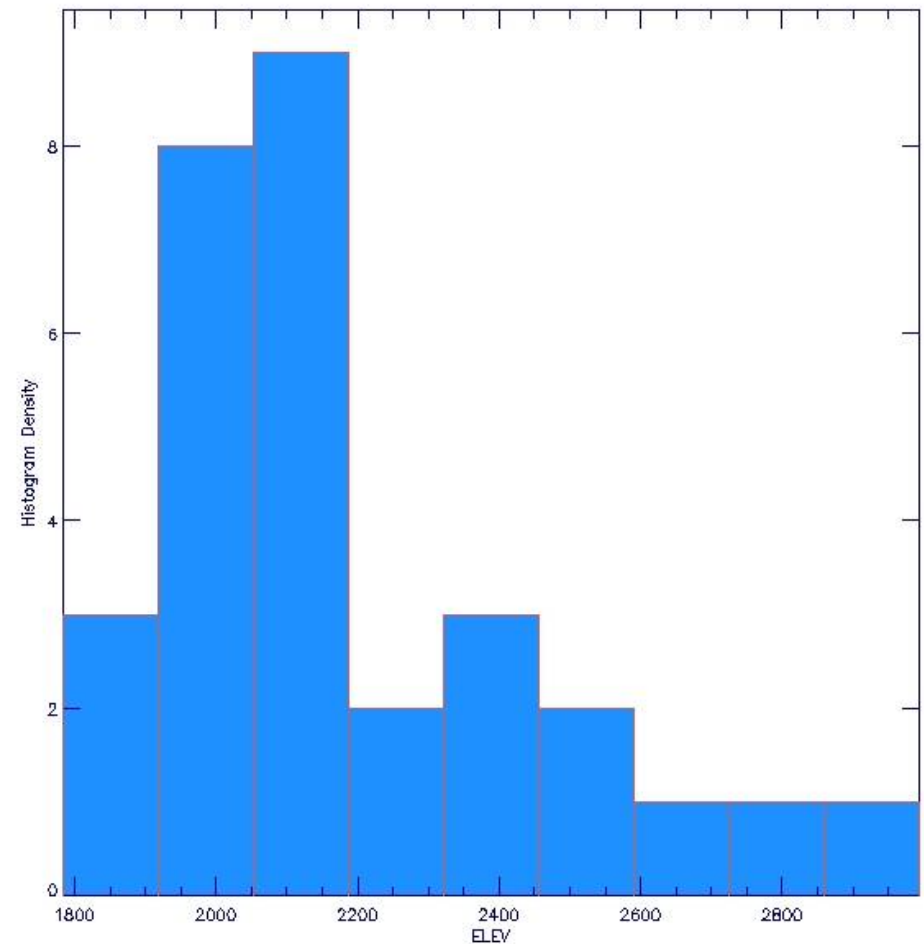
$$\text{SWE} = \text{SNOW HEIGHT} \times \text{SNOW DENSITY} \times \text{SNOW COVER EXTENT}$$

## SNOW DENSITY: from point measurements to distributed fields

in theory we can use the same modelling approach used for snow height

... in practice we have

...3) **bad distribution of measurement points**



$$\text{SWE} = \text{SNOW HEIGHT} \times \text{SNOW DENSITY} \times \text{SNOW COVER EXTENT}$$

## SNOW DENSITY: from point measurements to distributed fields

So we used **monthly means** of measured data ... one value applied on all Aosta Valley

Dec	2007	229 [Kgm <sup>-3</sup> ]
Jan	2007	242
Feb	2007	298
Mar	2007	324
Apr	2007	366
May	2007	390
...		
Nov	2008	205
Dec	2008	281
Jan	2009	310
Feb	2009	320
Mar	2009	351
Apr	2009	394



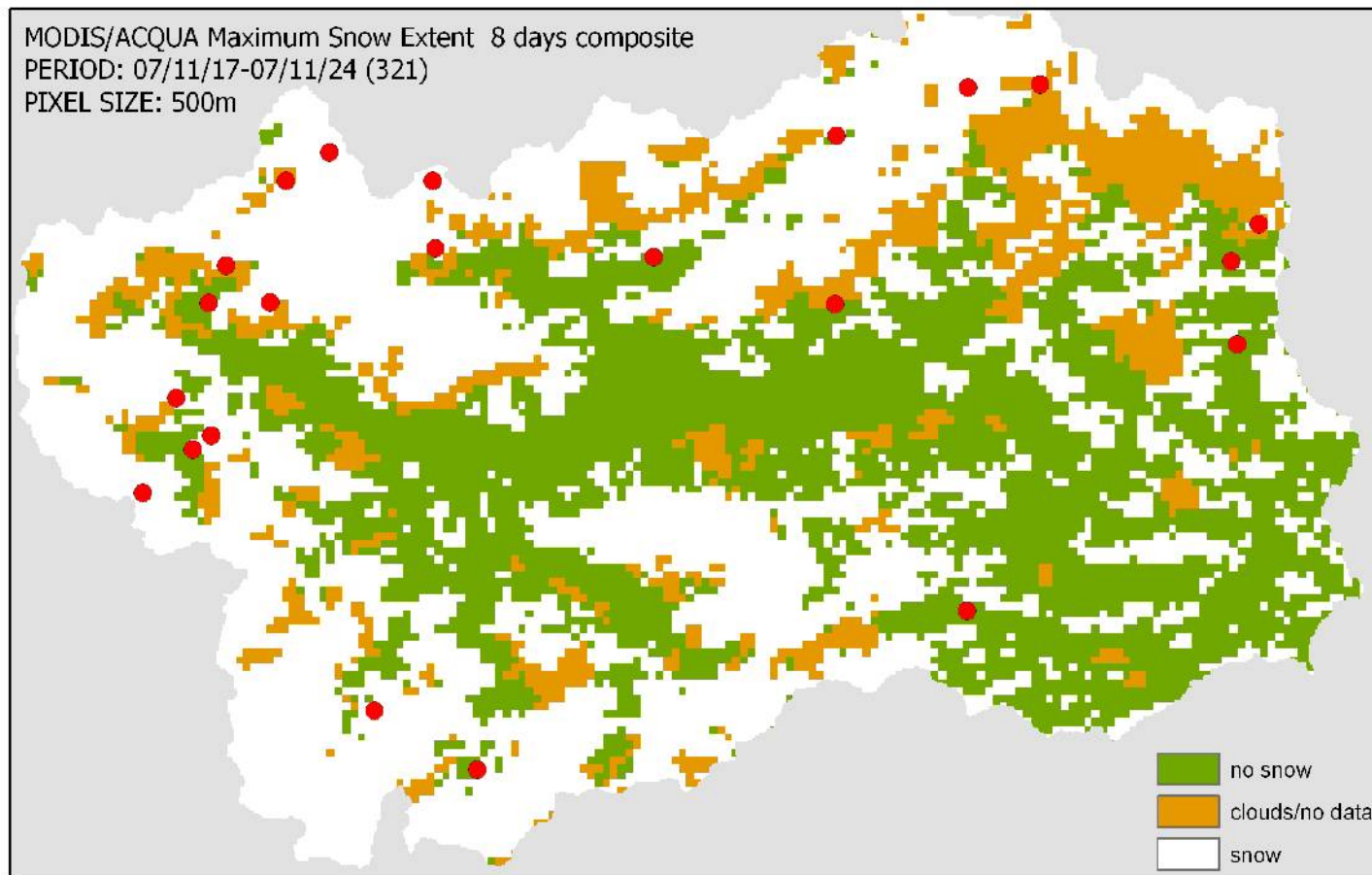
$$\text{SWE} = \text{SNOW HEIGHT} \times \text{SNOW DENSITY} \times \text{SNOW COVER EXTENT}$$

## MODIS SNOW COVER DATA: MOD10A2

Maximum snow cover extent

8 day composite

500 m spatial resolution

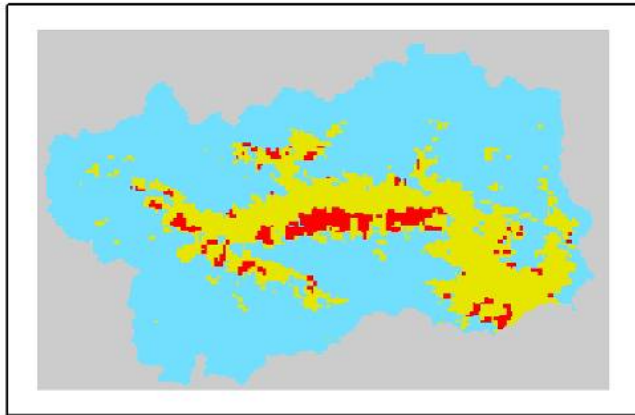


$$\text{SWE} = \text{SNOW HEIGHT} \times \text{SNOW DENSITY} \times \text{SNOW COVER EXTENT}$$

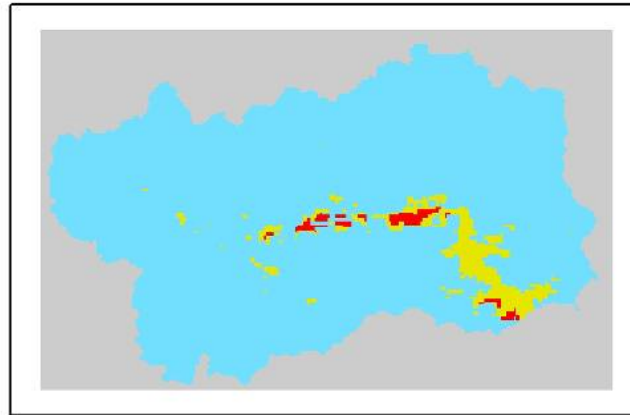
**MODIS SNOW COVER DATA: MOD10A2**

## Snow cover extent temporal evolution (early winter 2008)

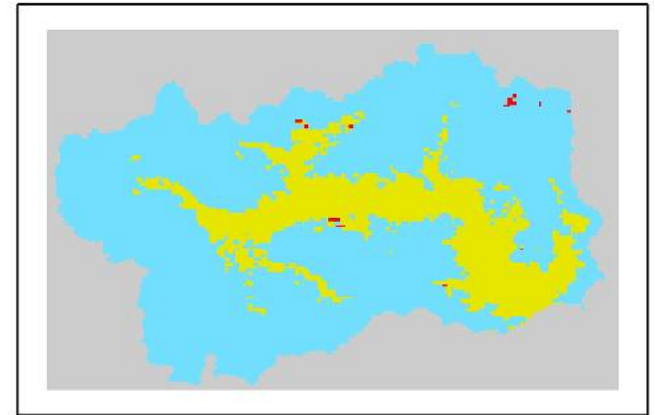
DECEMBER



JANUARY



FEBRUARY



**SWE** = SNOW HEIGHT x SNOW DENSITY x SNOW COVER EXTENT

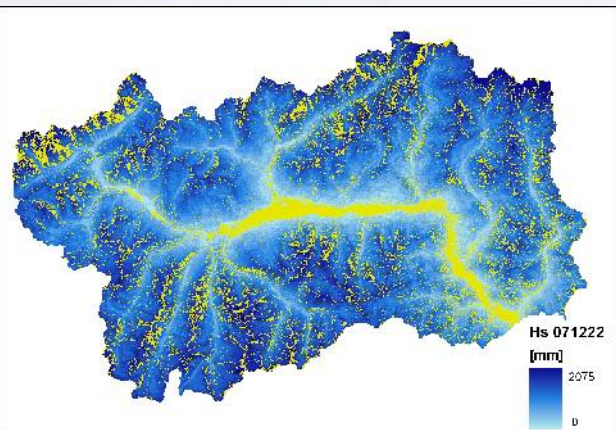


**Example: December 2007**

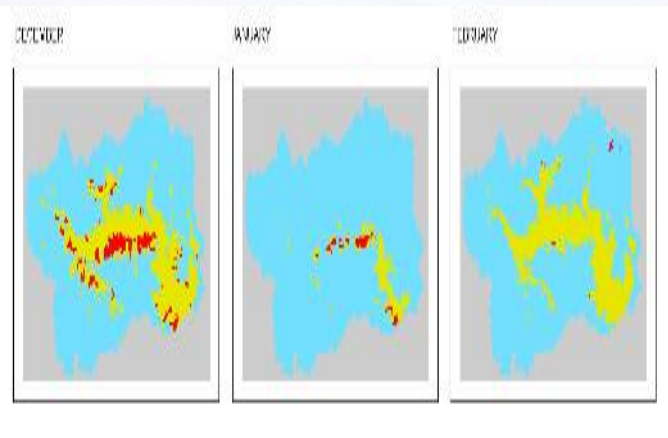
Snow Height x mean density value

Snow cover extent

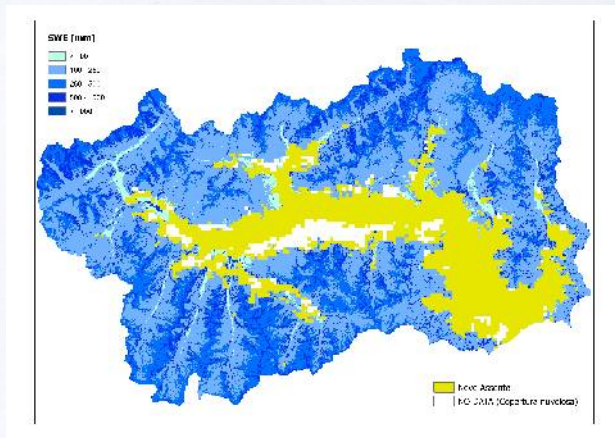
SWE



X



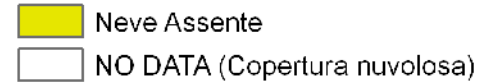
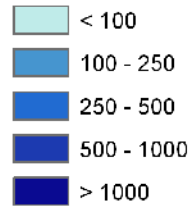
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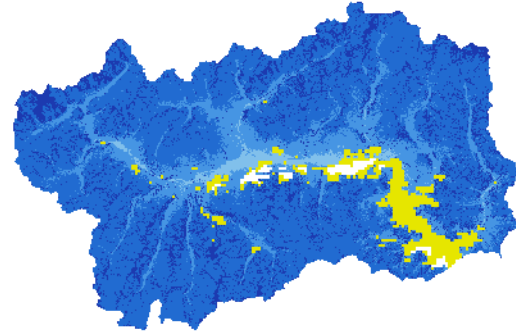
$$\text{SWE} = \text{SNOW HEIGHT} \times \text{SNOW DENSITY} \times \text{SNOW COVER EXTENT}$$

### EVOLUZIONE MENSILE DELLA QUANTITA' D'ACQUA CONTENUTA NELLA NEVE SUL TERRITORIO REGIONALE (inverno 2008)

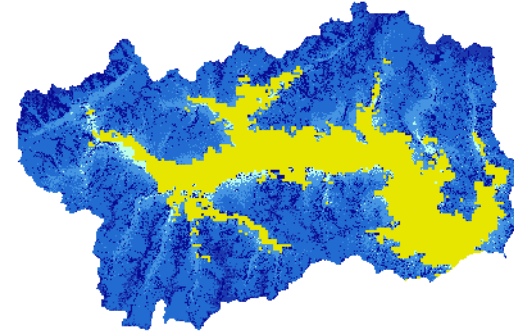
SWE [mm]



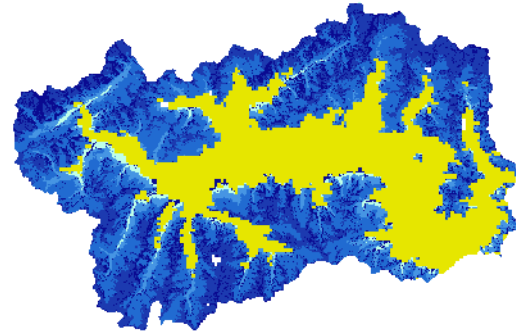
GENNAIO:  $821 \times 10^6 \text{ m}^3$



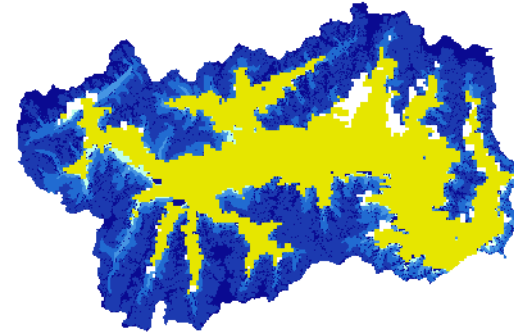
FEBBRAIO:  $720 \times 10^6 \text{ m}^3$



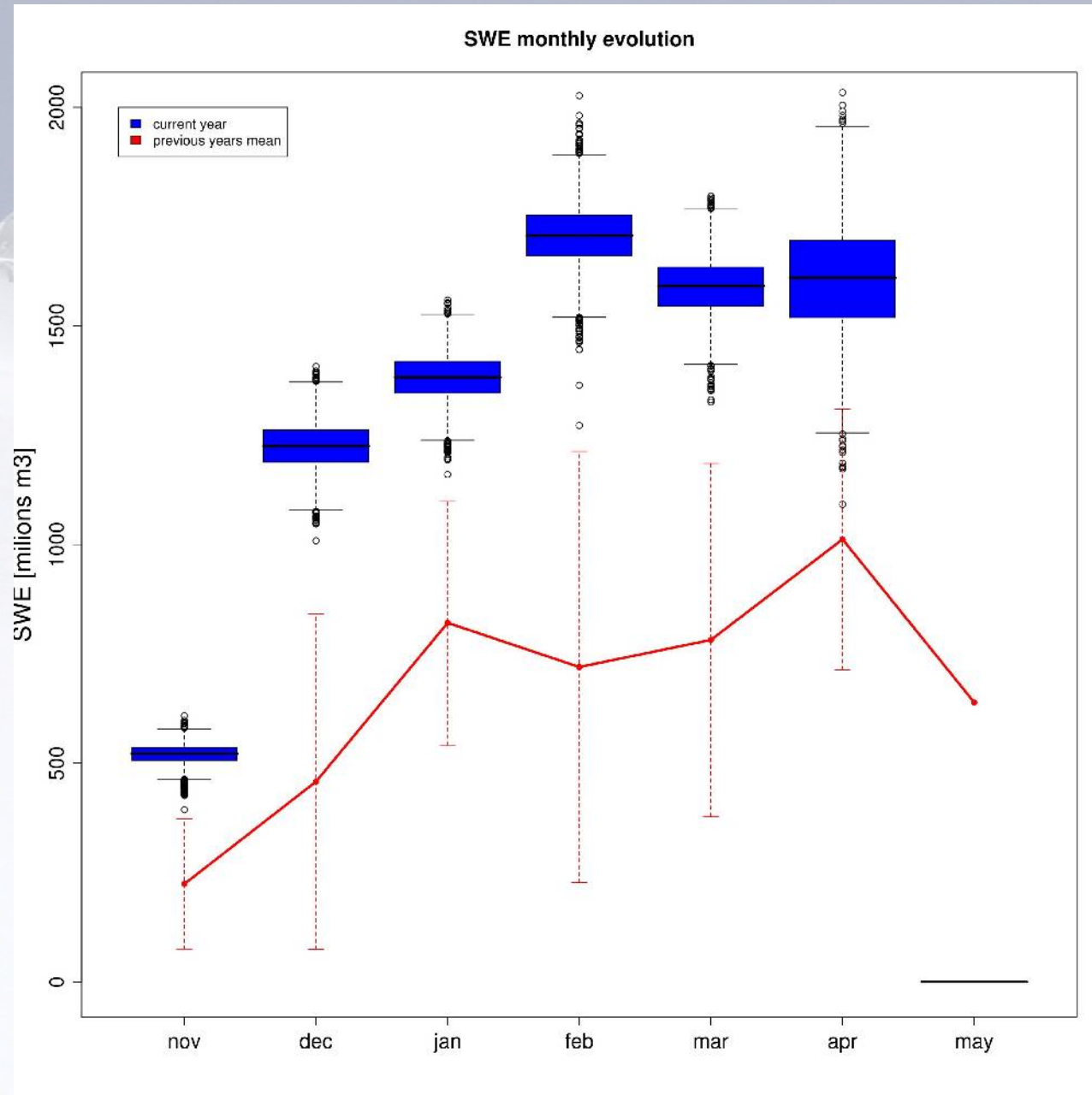
MARZO:  $782 \times 10^6 \text{ m}^3$



APRILE:  $1012 \times 10^6 \text{ m}^3$



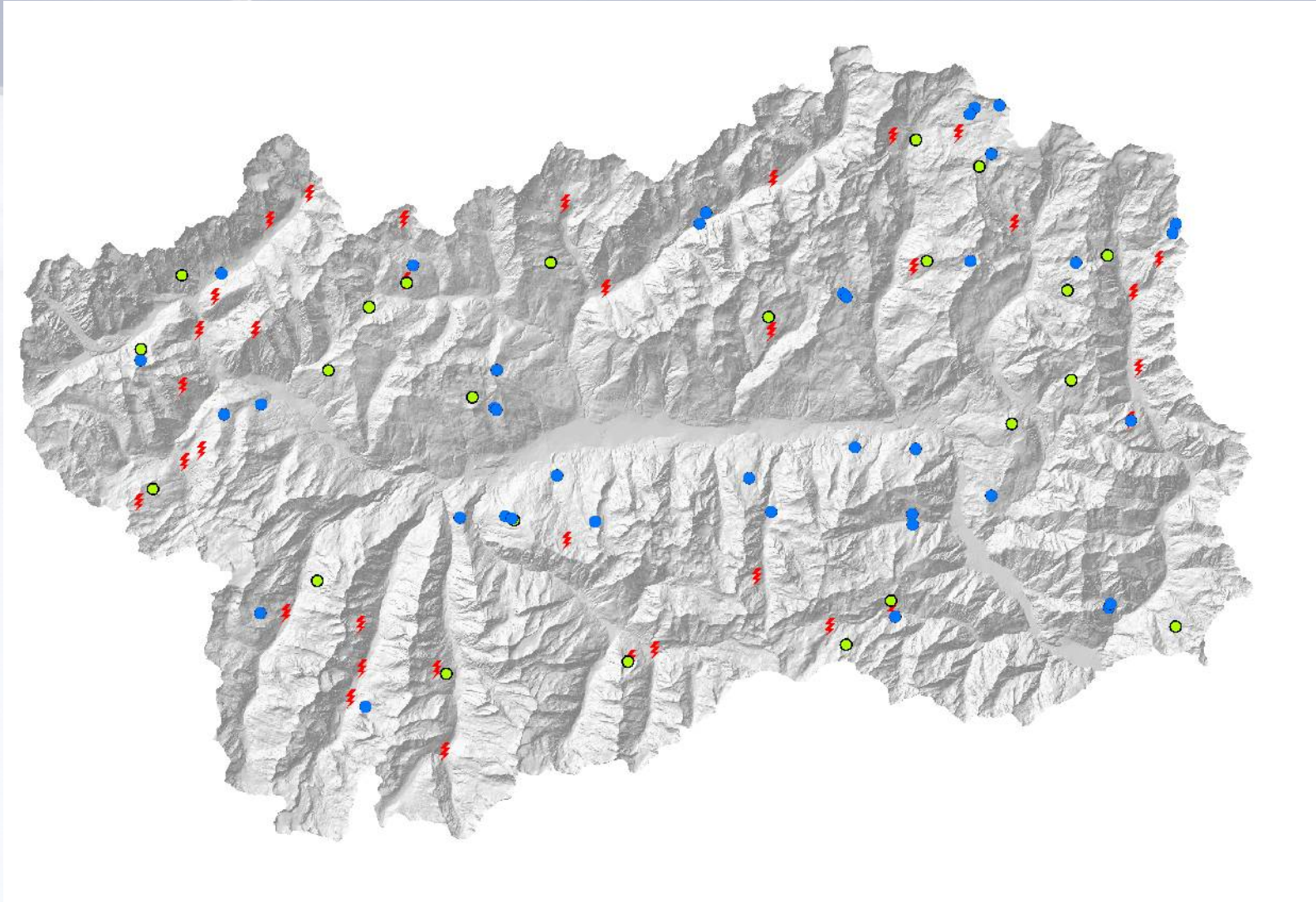
**SWE = SNOW HEIGHT x SNOW DENSITY x SNOW COVER EXTENT**



# SWE at regional scale future developments

**1) improve the network of snow density field measurements**

# SWE at regional scale future developments



# SWE at regional scale future developments

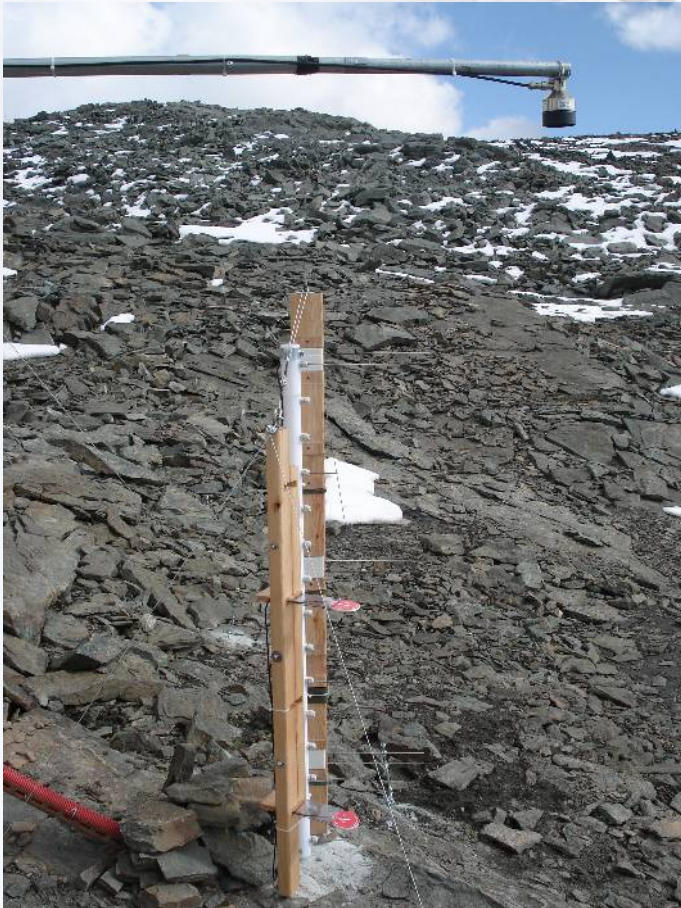
- 1) improve the network of snow density field measurements**
- 2) continuous measurements of parameters which can be related to snow density**



# SWE at regional scale future developments

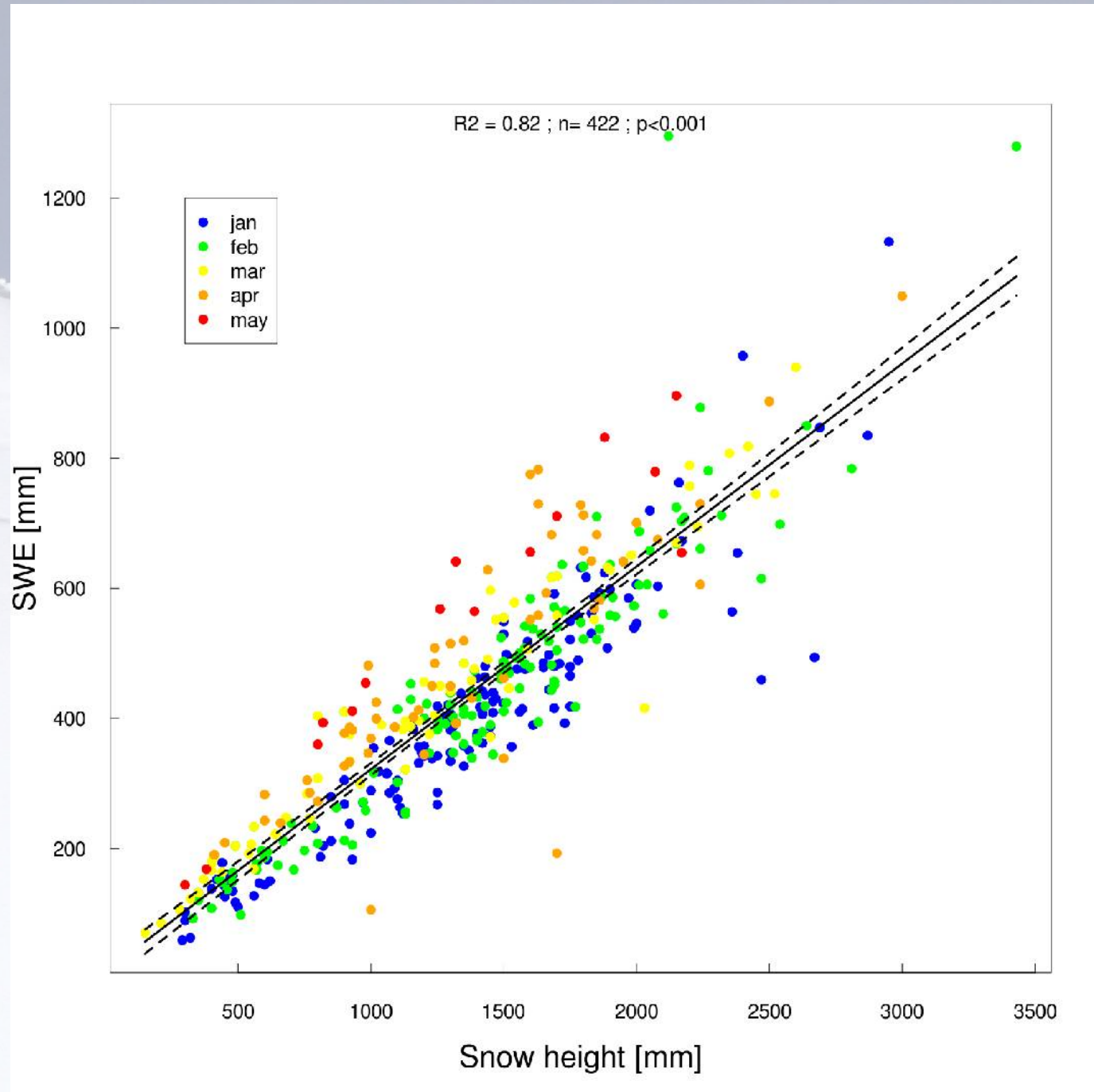
2) continuous measurements of **parameters which can be related to snow density:**

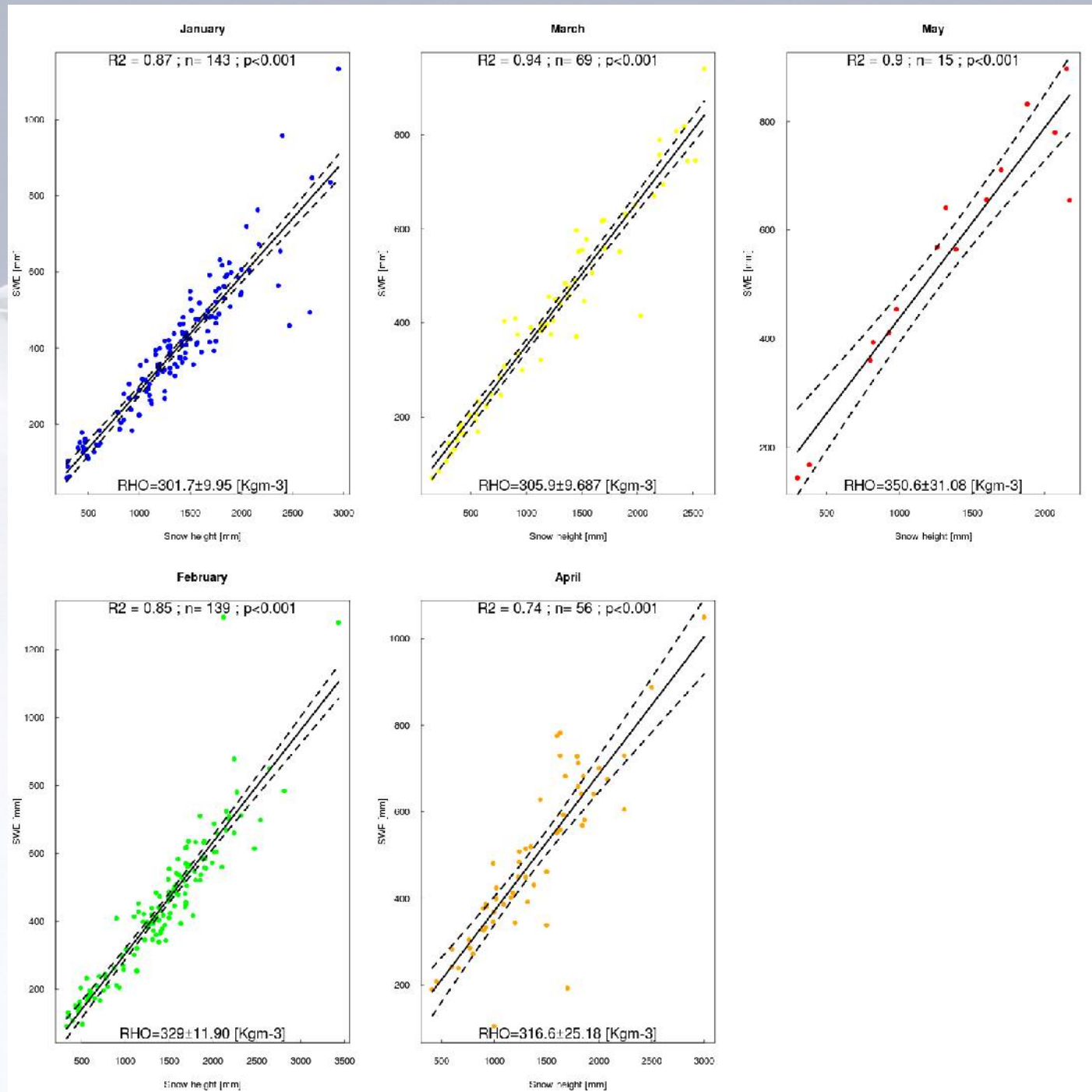
**CS616 – Water content reflectometer (sensors for soil humidity)**



## SWE at regional scale future developments

- 1) improve the network of **snow density field measurements**
- 2) continuous measurements of **parameters which can be related to snow density**
- 3) use of empirical relationships between **SWE and Snow Height**





## SWE at regional scale future developments

- 1) improve the network of **snow density field measurements**
- 2) continuous measurements of **parameters which can be related to snow density**
- 3) **temporal resolution** of the elaboration
- 4) retrieval of informations at **subpixel resolution** (unmixing + use of MOD10A1 FSC)
- 5) take into account the **effect of forest** on snow height and snow density

introduction

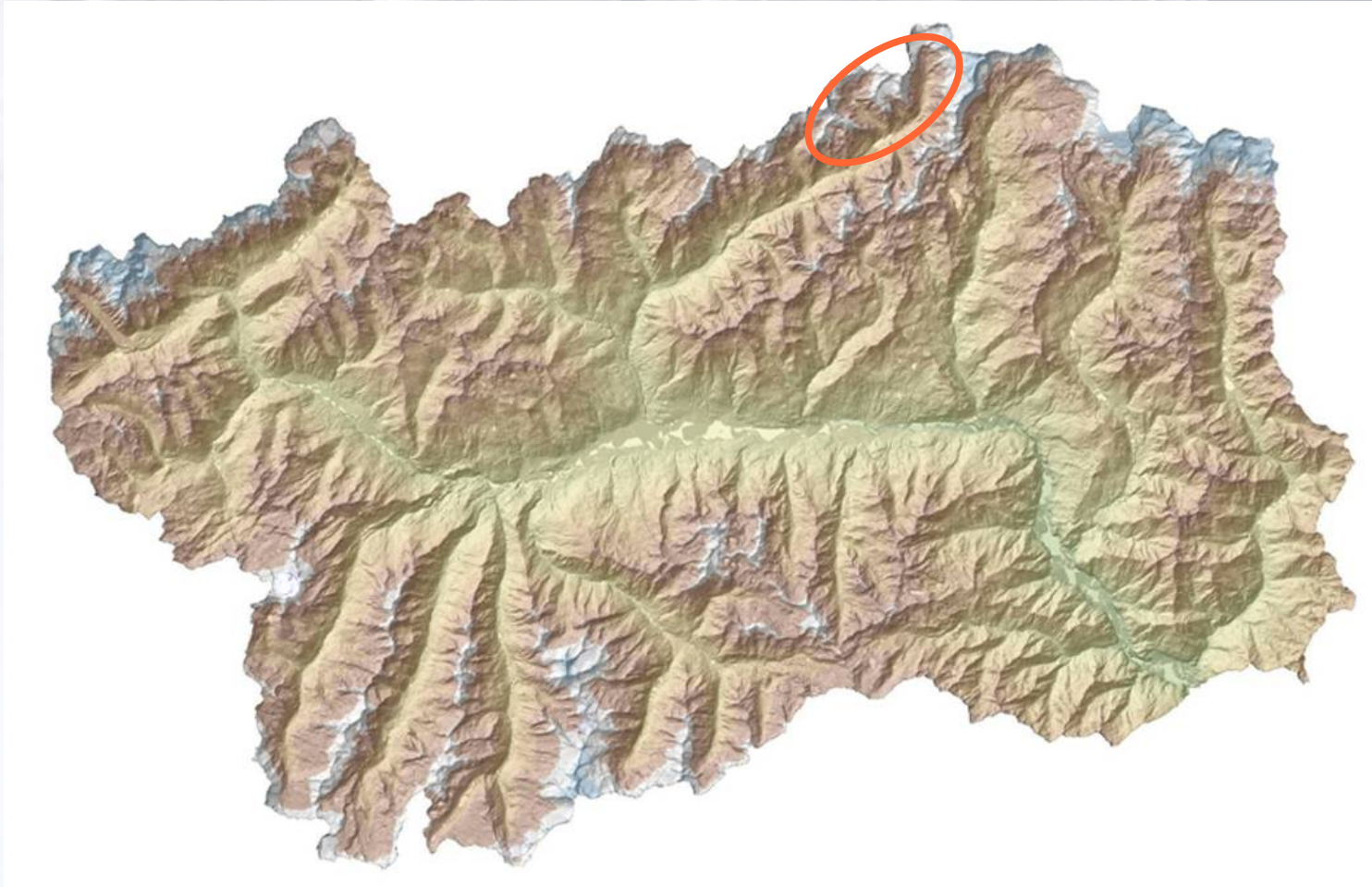
SWE distribution at regional scale (3000 Km<sup>2</sup>)

**SWE distribution at medium basin scale (120 Km<sup>2</sup>)**

melt modelling

## Valpelline (120 Km<sup>2</sup>):

basin with the biggest dam in the Aosta Valley (105 millions of m<sup>3</sup>)  
hydro power production (CVA spa)





## **SWE at medium scale**

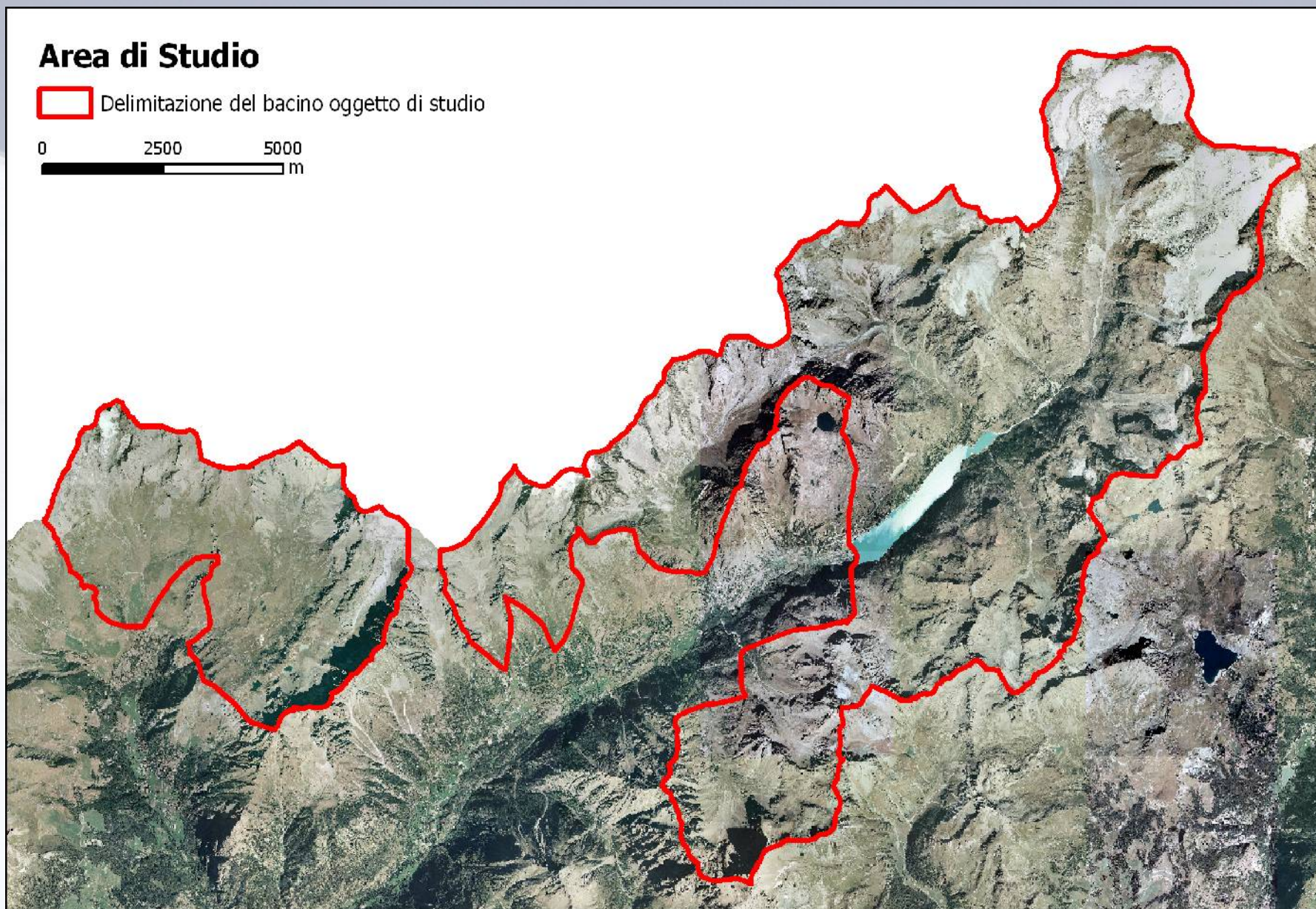
**the aim is to know the total amount of water stored in snow at the beginning of the melting season (late may – june)**

**The estimation of SWE is coupled with the application of a distributed melt model**

**it's used to plan and optimise hydro power production**



# Valpelline (120 Km<sup>2</sup>)



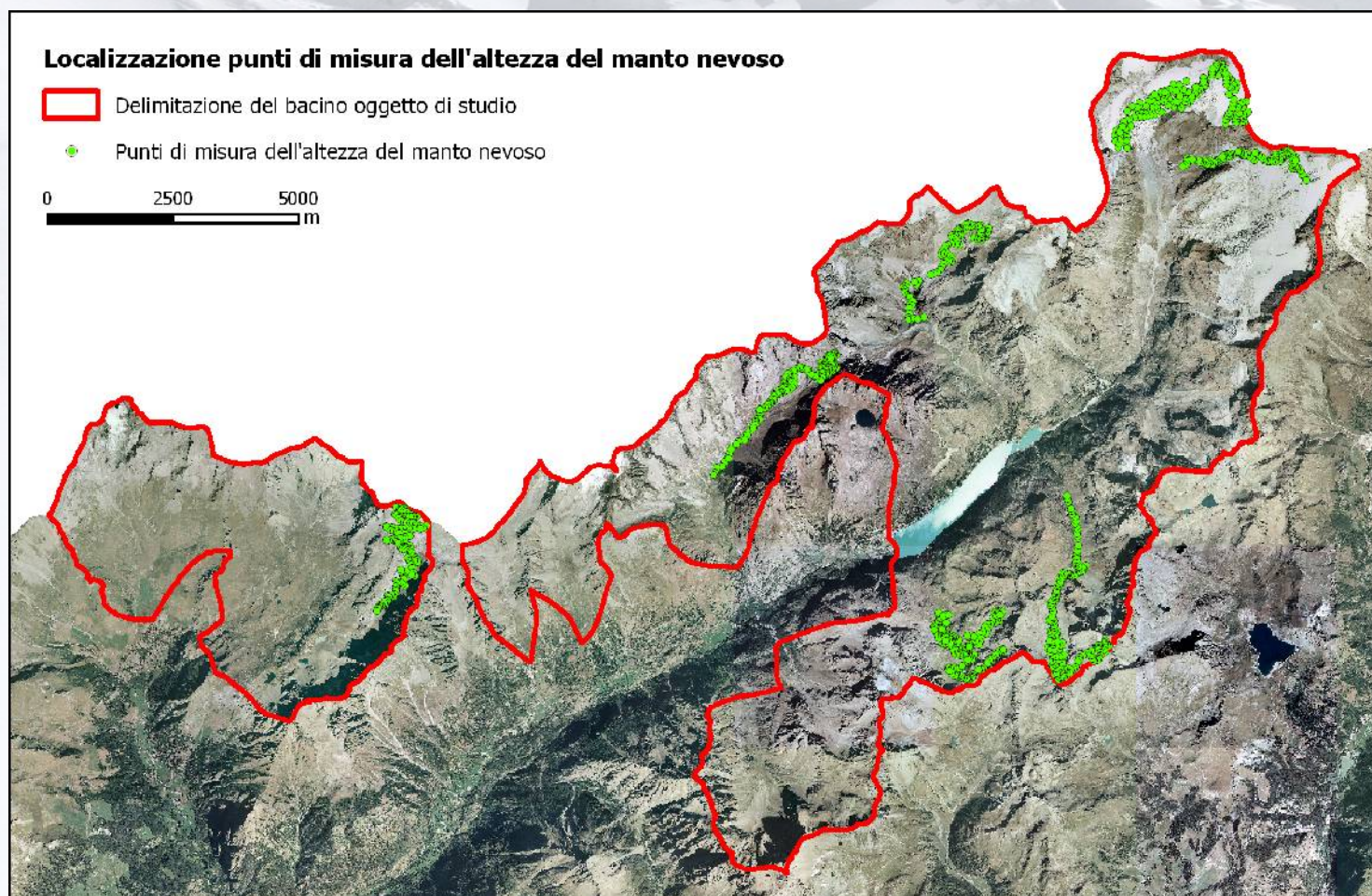
## Valpelline (120 Km<sup>2</sup>)

- SWE is modelled for late spring (maximum accumulation)
- DATA SET: single field campaign (measures of snow height and snow density)



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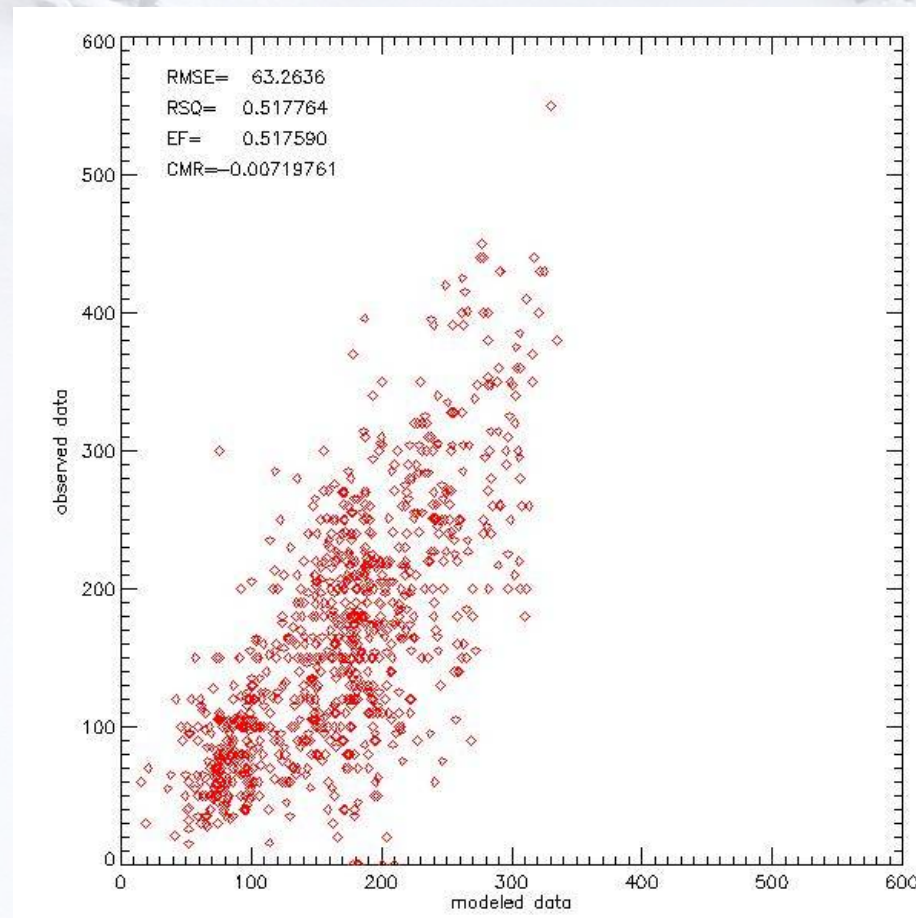


## Valpeline (120 Km<sup>2</sup>)

**SWE is modelled with the same method used at regional scale but:**

**1) we have better distributions of point measurements**

**2) we have a bigger number of sampling points (900 SH data + 30/40 SD data)**



## Valpelline (120 Km<sup>2</sup>)

**SWE is modelled with the same method used at regional scale but:**

- 1) we have better distributions of point measurements**
- 2) we have a bigger number of sampling points (900 SH data + 30/40 SD data)**
- 3) we can distribute SD data as well (avoiding the use of a mean)**
- 4) SCA can be estimated by:**
  - the photo interpretation of oblique terrestrial images collected during field campaign**
  - using MODIS FSC data (MOD10A2) ... but the spatial resolution can be too coarse**

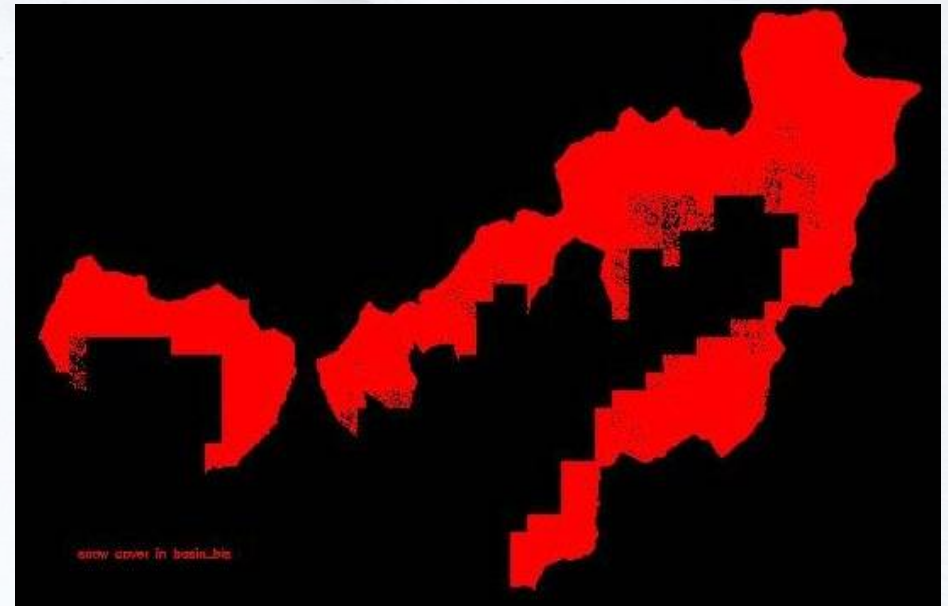
## Valpelline (120 Km<sup>2</sup>):

**SWE is modelled with the same method used at regional scale but:**

**2008 SCA: photo interpretation**

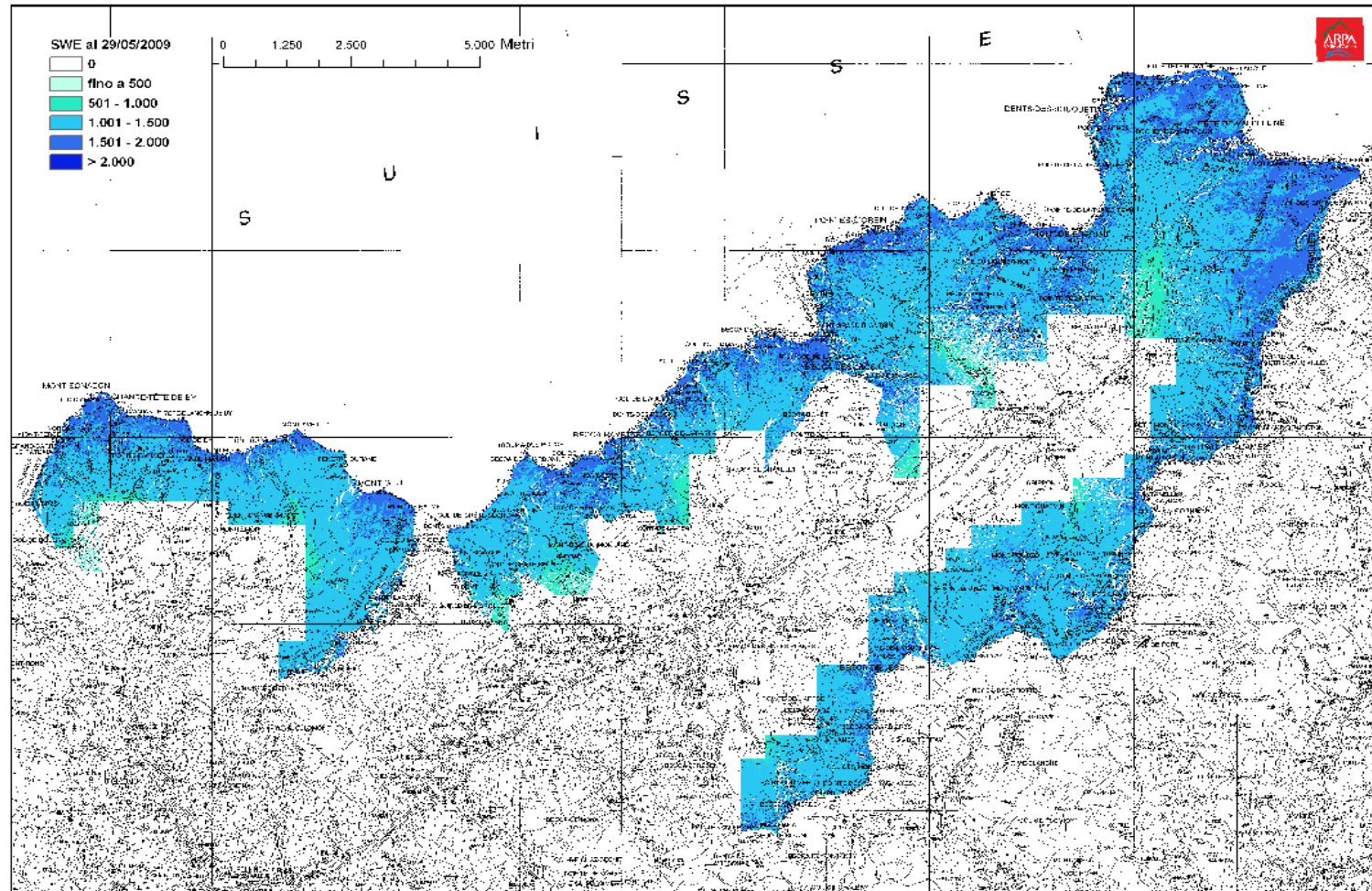


**2009 SCA: MOD10A1 FSC**



## Valpeline (120 Km<sup>2</sup>):

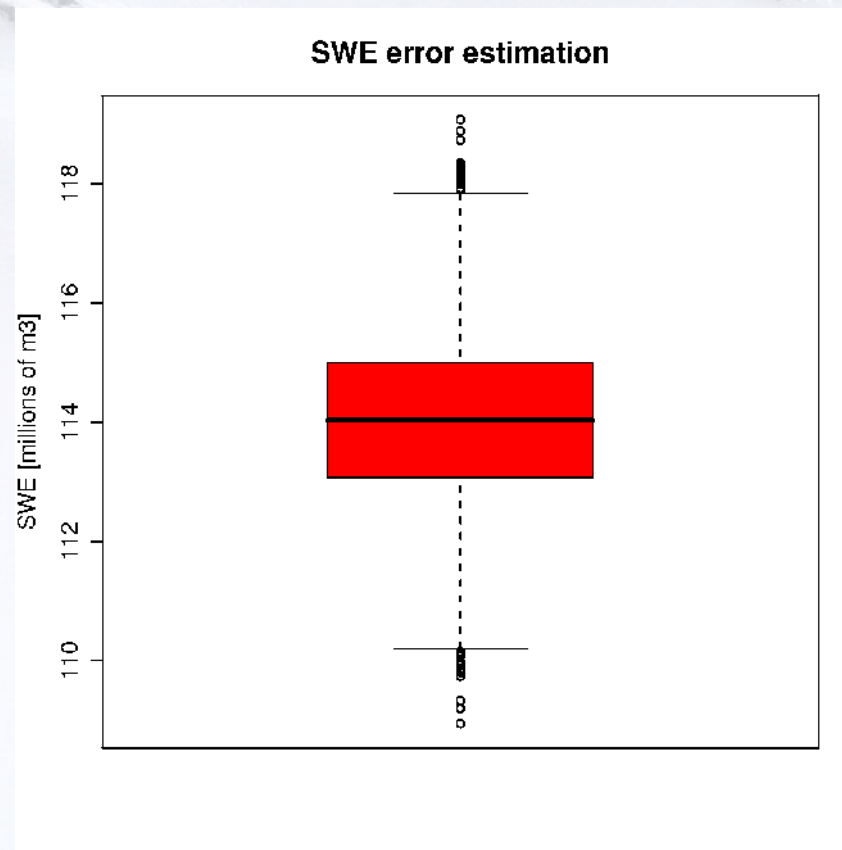
$$\text{SWE} = \text{SNOW HEIGHT} \times \text{SNOW DENSITY} \times \text{SNOW COVERED AREA}$$



## Valpeline (120 Km<sup>2</sup>):

$$\text{SWE} = \text{SNOW HEIGHT} \times \text{SNOW DENSITY} \times \text{SNOW COVERED AREA}$$

25/05/2009 SWE





**introduction**

**SWE distribution at regional scale (3000 Km<sup>2</sup>)**

**SWE distribution at medium basin scale (120 Km<sup>2</sup>)**

**melt modelling**

# **Snow and Glaciers melt modelling in Valpelline**

**ETI model: Distributed Enhanced Temperature-Index Melt Model (ETI)  
including the Shortwave radiation balance (Pellicciotti et al 2004, JoG)**



## Snow and Glaciers melt modelling in Valpelline

**ETI model: Distributed Enhanced Temperature-Index Melt Model (ETI) including the Shortwave radiation balance (Pellicciotti et al 2004, JoG)**

$$M = T_f \cdot T + A F \cdot (1 - \alpha) \cdot I \quad T > T_t$$

**T: air temperature**

**I: shortwave incoming radiation**

**$\alpha$ : albedo**

**The model melts snow/ice when air temperature is above 1°C ( $T_t$ ).**

**Melt rate is determined by air temperature, shortwave incoming radiation and albedo**

**INPUT DATA:**

- 1) air temperature**
- 2) precipitation**
- 3) initial SWE**

# Snow and Glaciers melt modelling in Valpelline

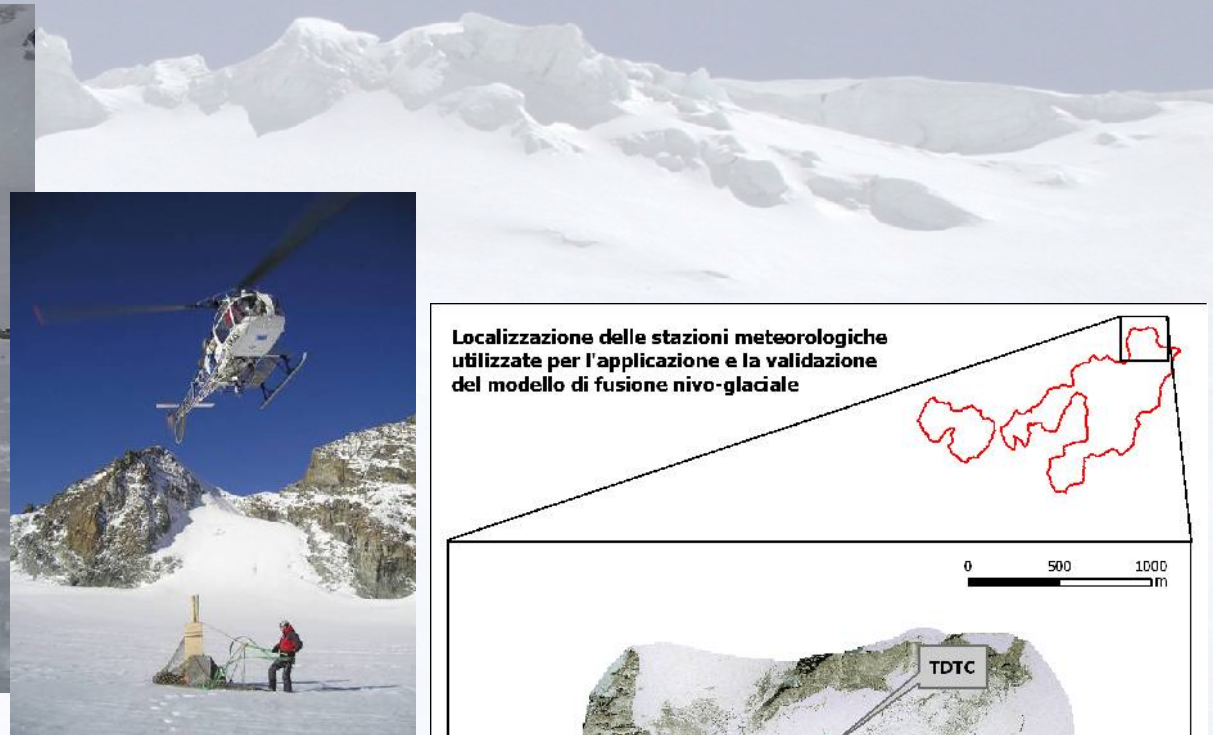
**ETI model: Distributed Enhanced Temperature-Index Melt Model (ETI) including the Shortwave radiation balance (Pellicciotti et al 2004, JoG)**



# Snow and Glaciers melt modelling in Valpelline

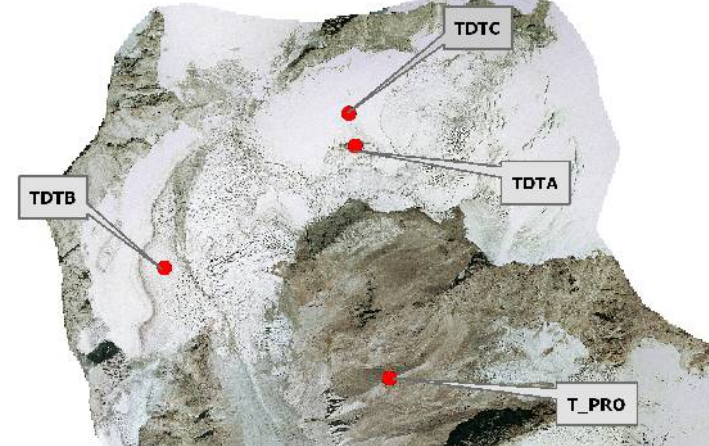
2006 application on Tza de Tzan glacier

2007 + 2008 application on entire basin



Localizzazione delle stazioni meteorologiche utilizzate per l'applicazione e la validazione del modello di fusione nivo-glaciale

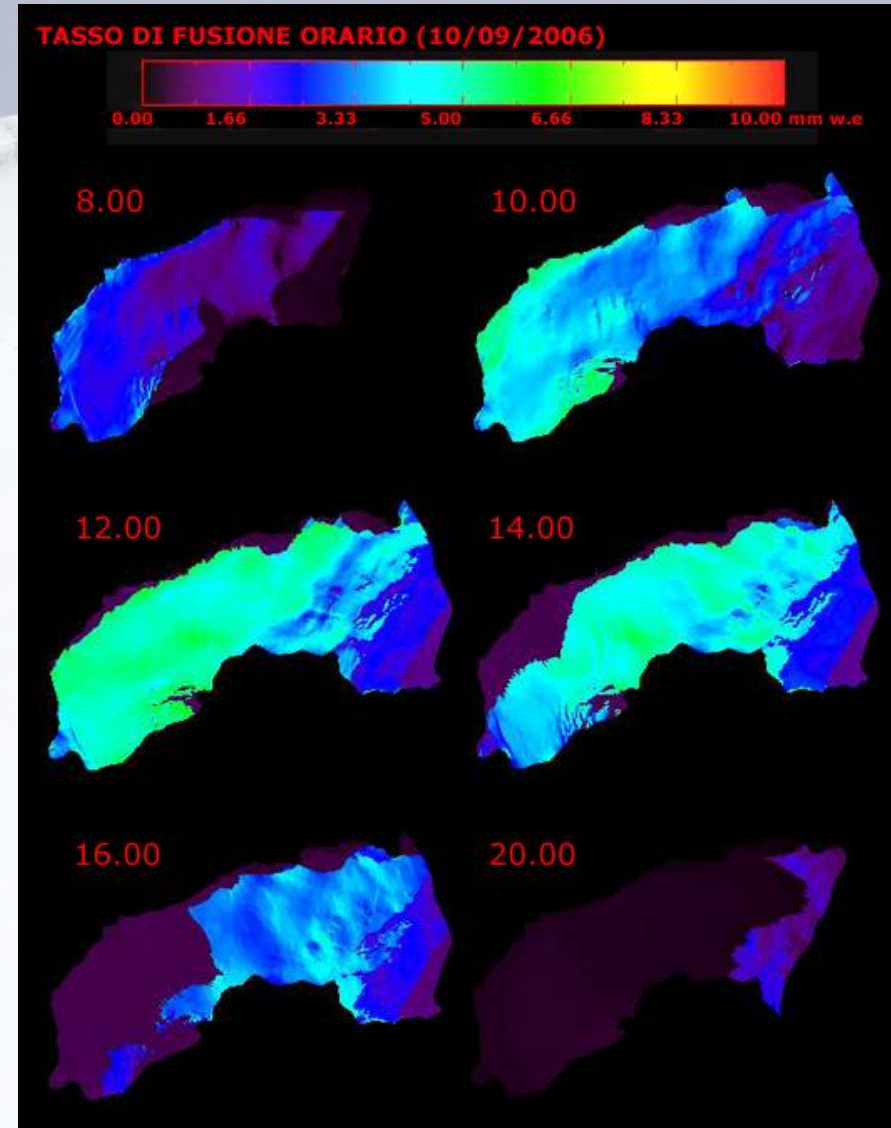
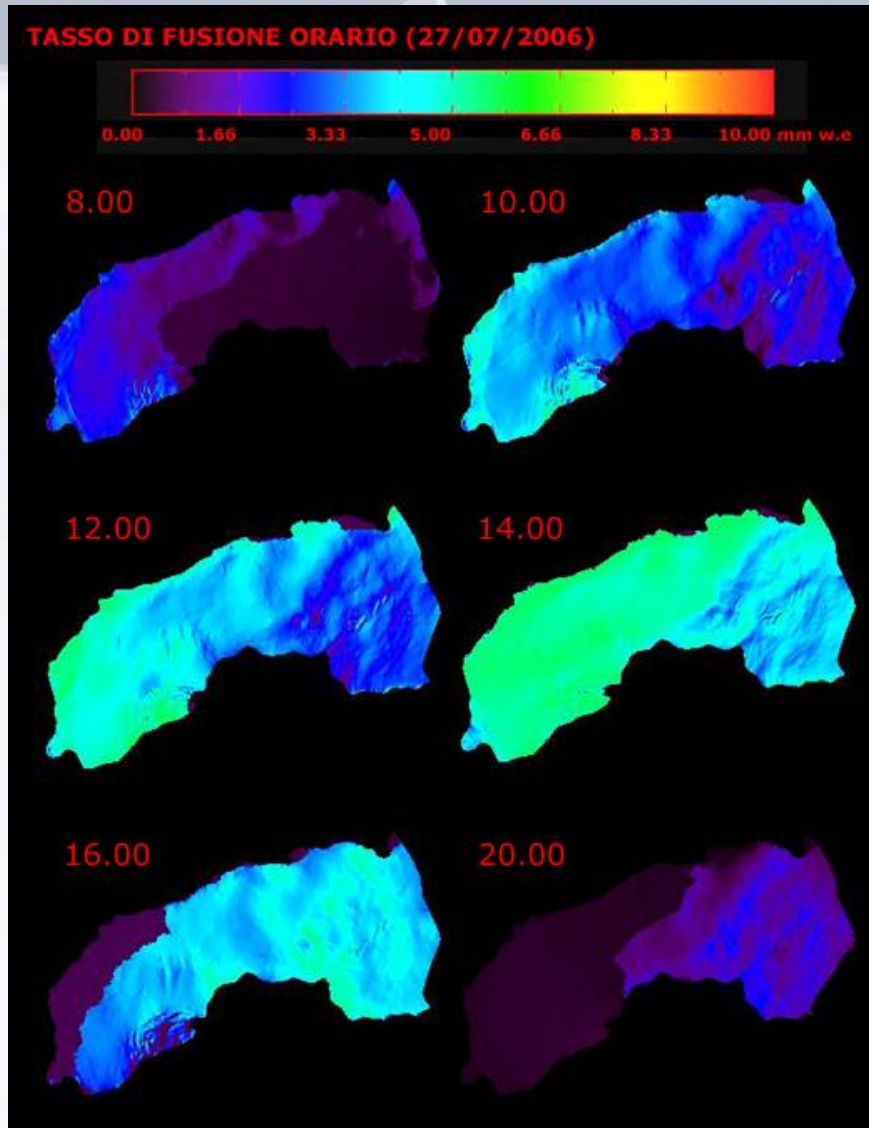
0 500 1000 m



Weather station installation and ablation measurements during summer (UDG and stakes)

# Snow and Glaciers melt modelling in Valpelline

## 2006 application on Tza de Tzan glacier: examples of model output



# Snow and Glaciers melt modelling in Valpelline

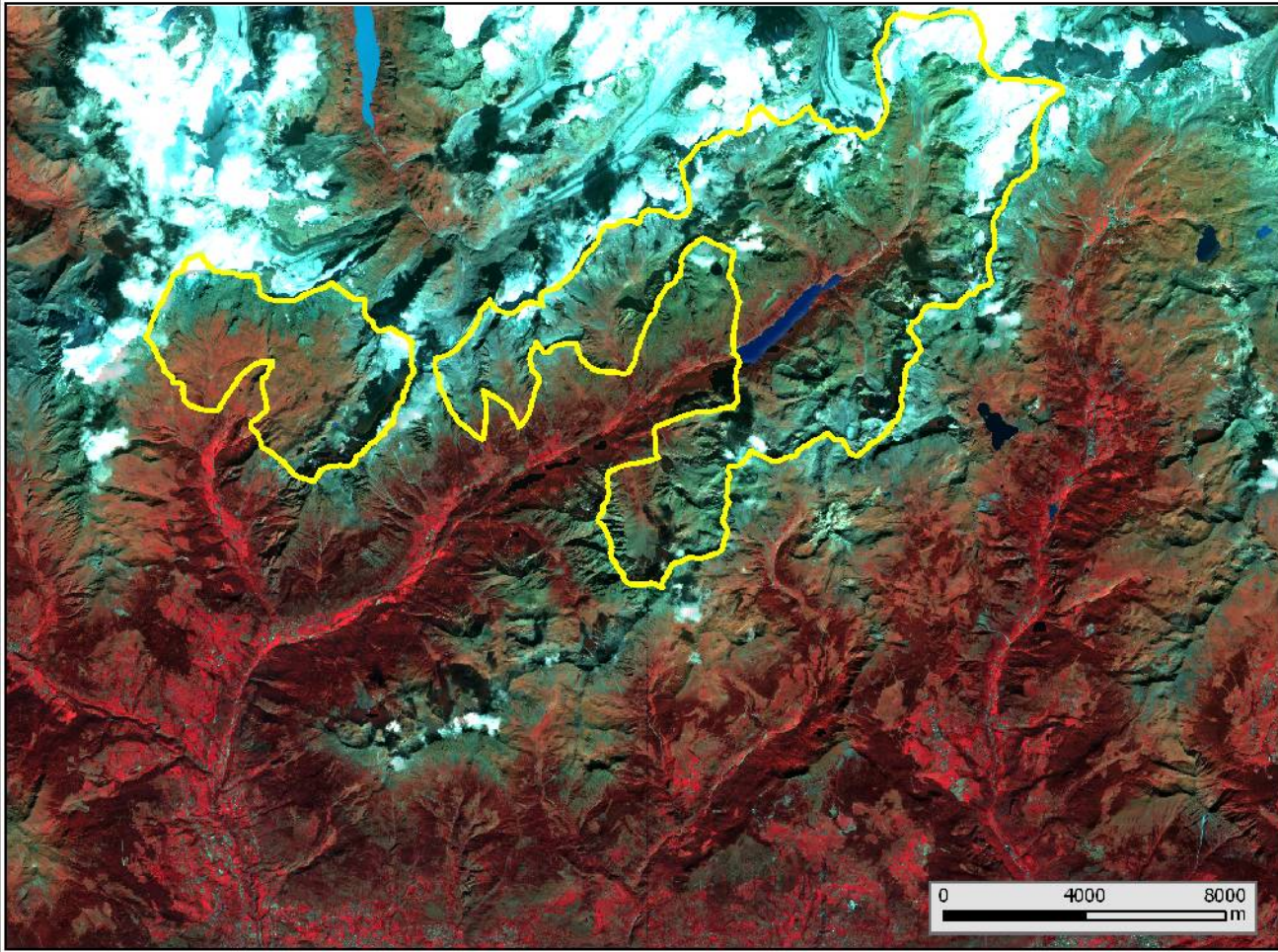
## 2006 application on Tza de Tzan glacier: model validation

- 1) Ablation Stakes and AWS measurements**
- 2) Snow cover extent during ablation season**
- 3) Discharge measurements made by CVA (hydro-power company)**

# Snow and Glaciers melt modelling in Valpelline

## 2006 application on Tza de Tzan glacier: model validation

Immagine SPOT del 24/09/07 utilizzata per la delimitazione della copertura nevosa  
(composizione IRFC)



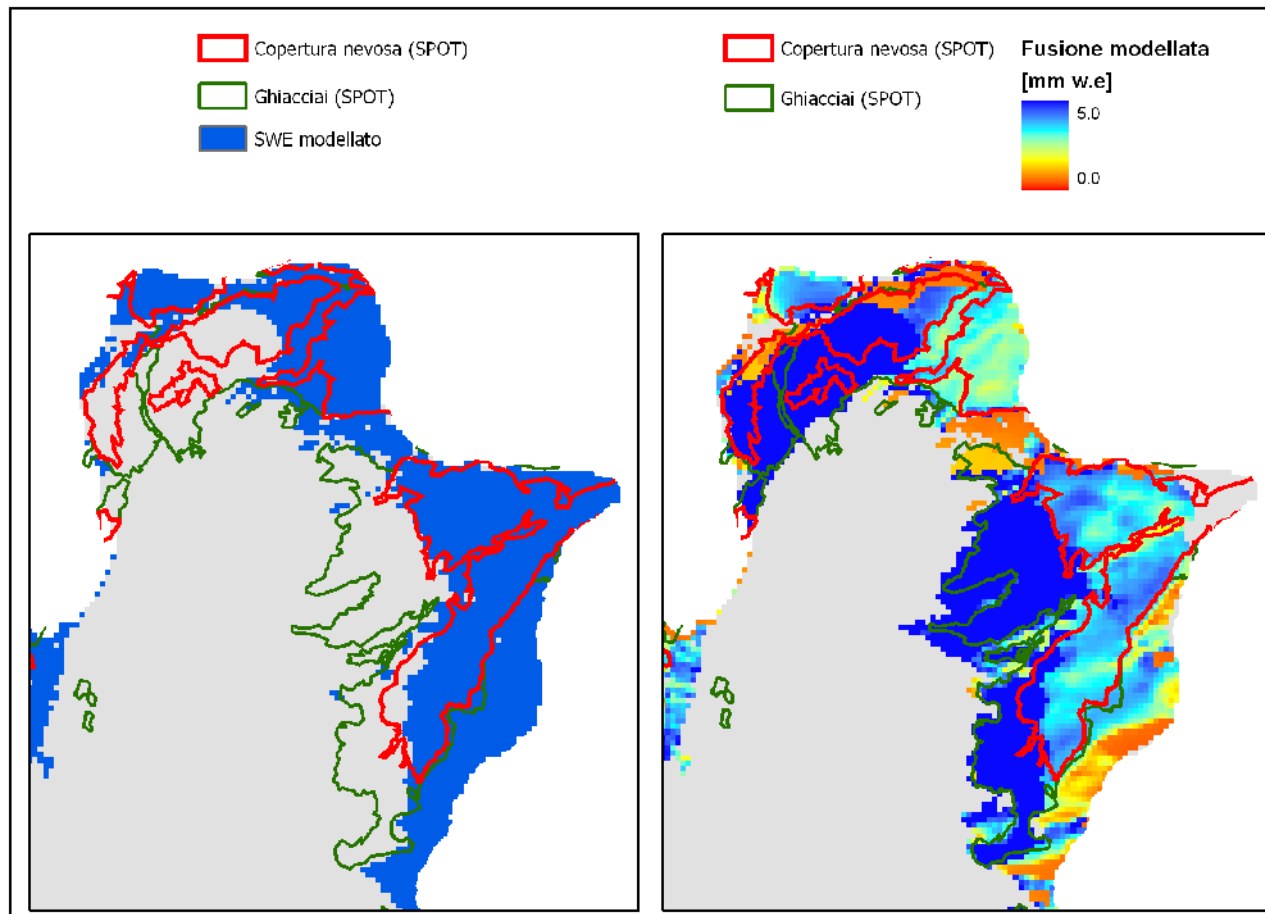
**Snow cover extent  
during ablation season:**

**high resolution SPOT  
image**



# Snow and Glaciers melt modelling in Valpelline

## 2006 application on Tza de Tzan glacier: model validation

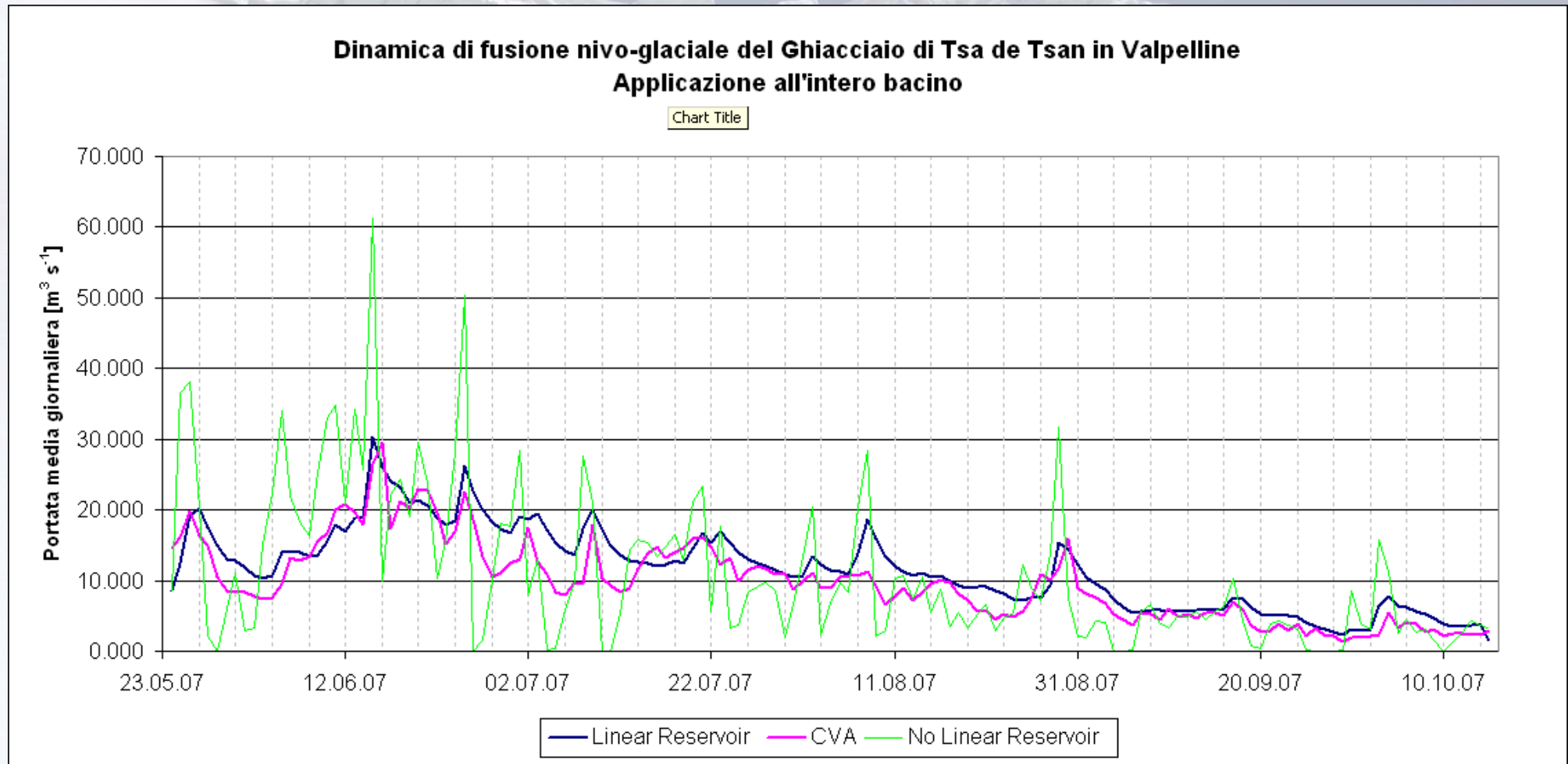


**Snow cover extent during ablation season:**

**high resolution SPOT image**

# Snow and Glaciers melt modelling in Valpelline

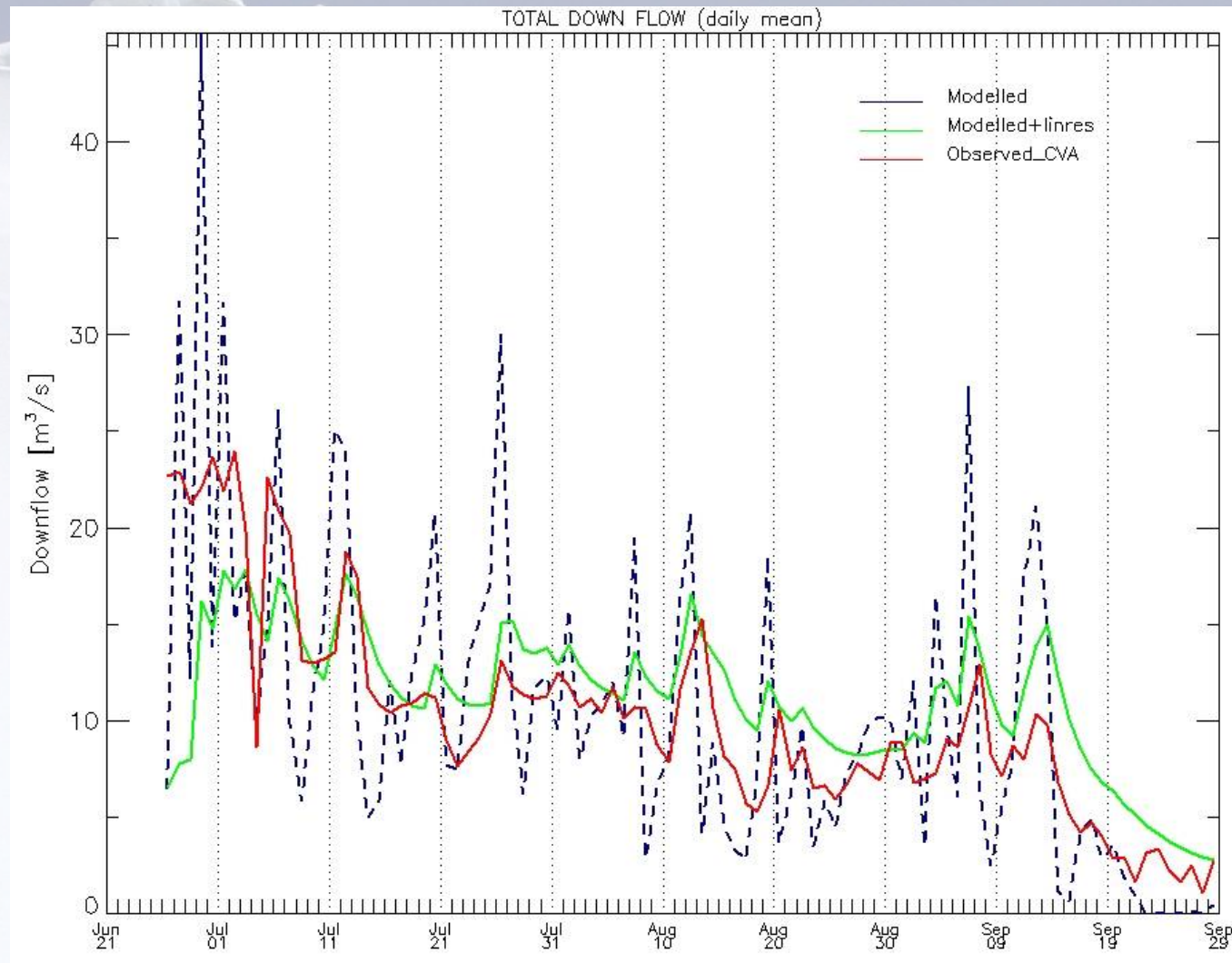
**2007 application on the entire basin.  
Daily discharge measured by CVA: model validation**



# Snow and Glaciers melt modelling in Valpelline

2008 application on the entire basin.

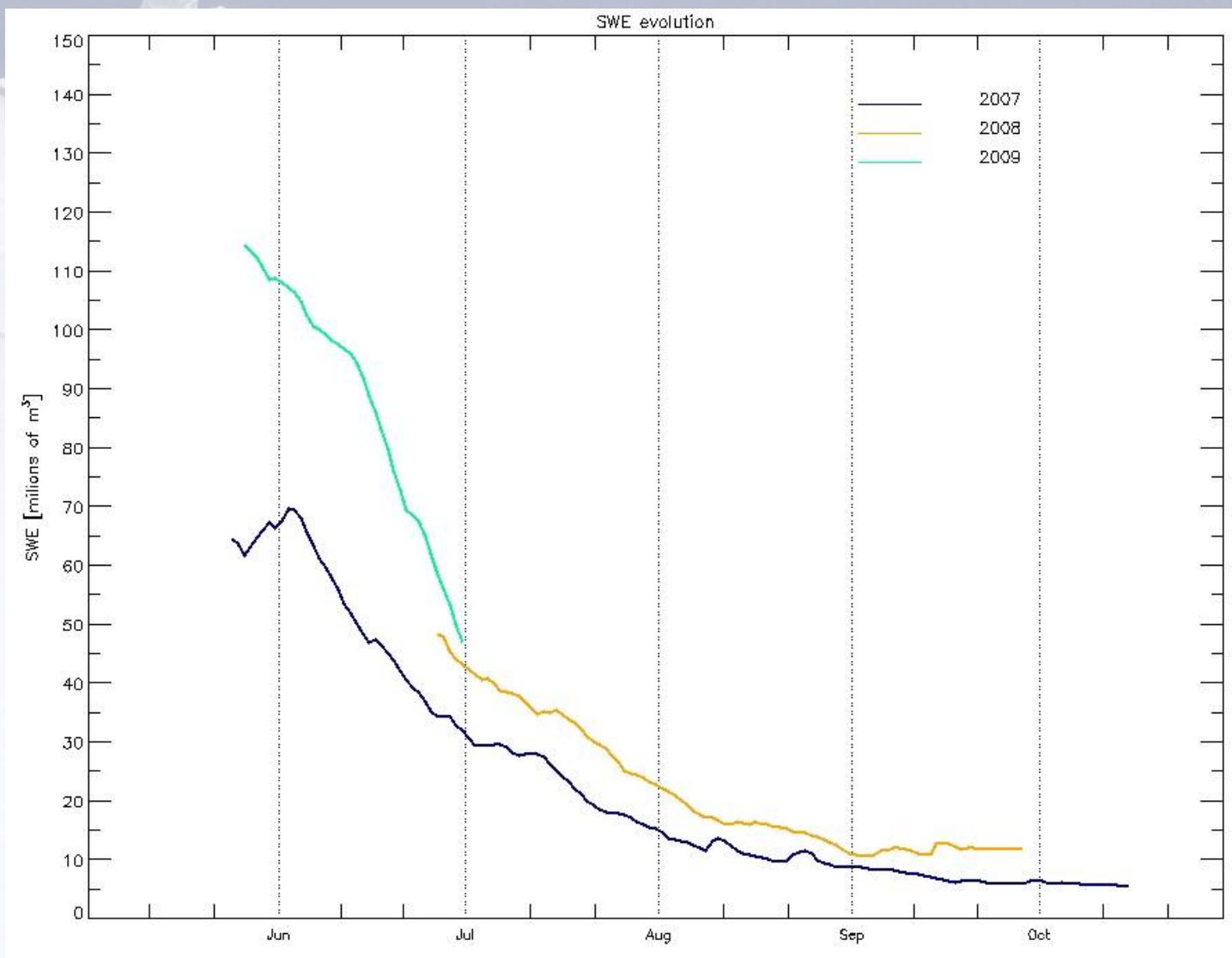
Daily discharge measured by CVA: model validation



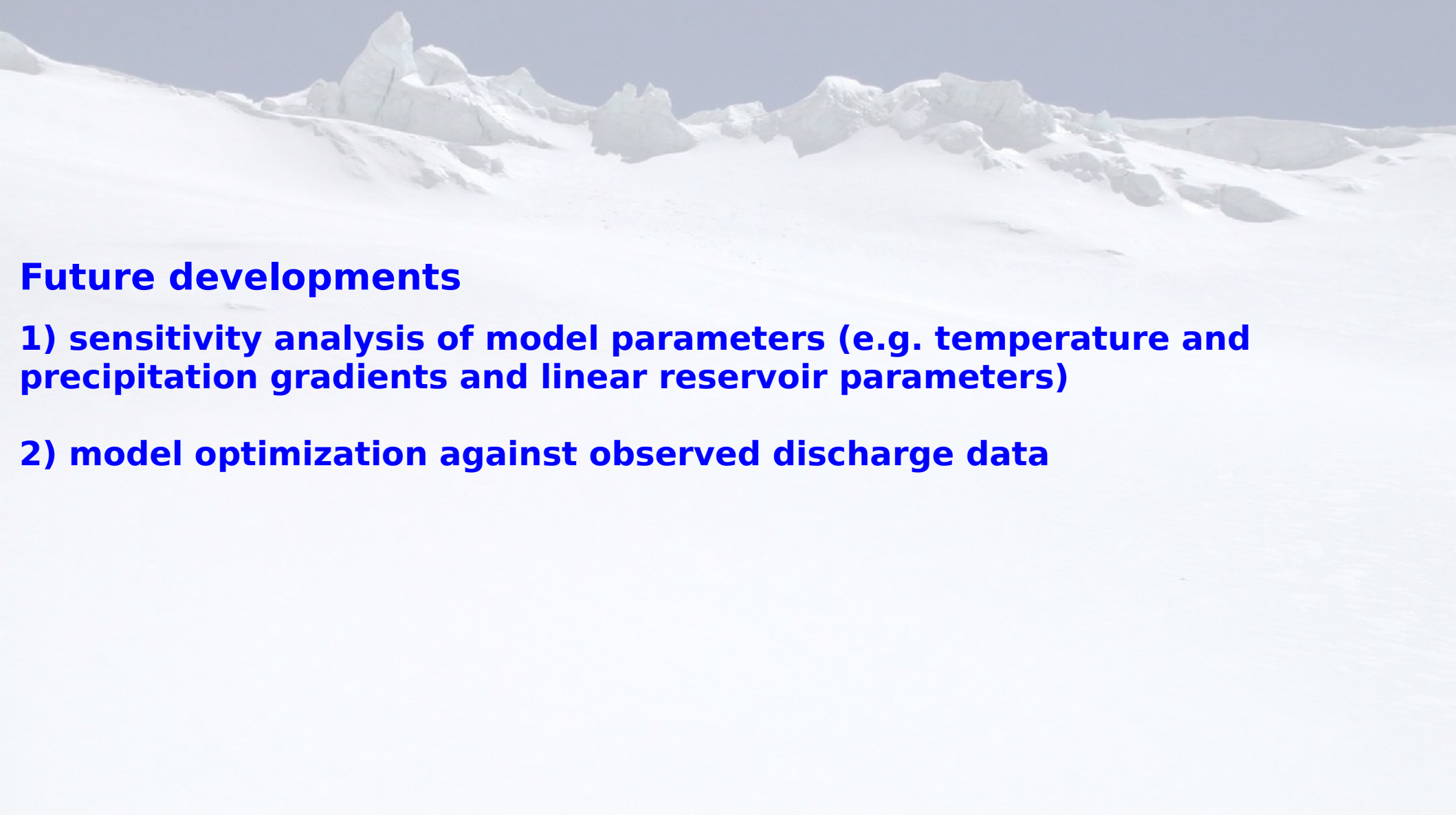
# Snow and Glaciers melt modelling in Valpelline

## SWE evolution on the entire basin

(preliminary results including 2009 snowy winter)



# Snow and Glaciers melt modelling in Valpelline



## Future developments

- 1) sensitivity analysis of model parameters (e.g. temperature and precipitation gradients and linear reservoir parameters)**
- 2) model optimization against observed discharge data**



**... thank you**